

# **Theory Construction and Causal Modeling**

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**Silver School of Social Work**  
**New York University**

# Overview

**First half of workshop will focus on theory construction using causal concepts. It will have a conceptual focus**

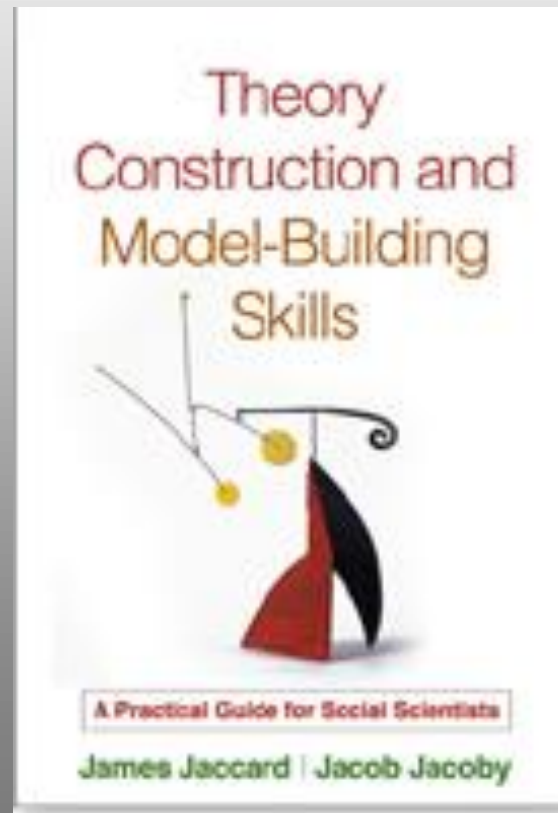
**Second half of the workshop will focus on the statistical analysis of causal theories using limited information estimation frameworks**

**I assume you have working knowledge of multiple regression and hypothesis testing**

# **Theory Construction**

# Theory Construction

**Focus is on the practical mechanics of constructing theory rather than philosophy of science**



# Causal Theories

**Most (but not all) theories rely heavily on the concept of causality, i.e., we seek to identify the *determinants* of a behavior or mental state and/or the *consequences* of a behavior or environmental/mental state**

- **Why do some people suffer from depression and others do not?**

**What are the causes of depression?**

- **Why do some people engage in unsafe sex while other people do not engage in unsafe sex? What are the causes of sexual risk behavior?**
- **Why do some people make use of mental health services but other people do not? What are the causes of service utilization?**

# Causal Theories

**Sometimes instead of *causes*, we are more interested in the *effects* of experiences or behaviors, but this is still part of causal analysis**

- What are the effects on a child of being raised by parents who are physically abusive?**
- What are the effects of being adopted on a person's mental health?**
- What are the effects of participating in a program to reduce stress on one's health?**

# **Building Causal Theories**

# Theory Construction

**All causal theories work with *variables* and presumed *causal relationships* between variables.**

**The first step in constructing a causal theory is to identify the phenomena you want to understand or the variable whose variability you want to explain**

**Unintended pregnancy**

**Alcohol abuse and drunk driving**

**Child anxiety**



# **Choosing an Outcome Variable**

**Choice of an outcome is often impacted by**

- Your values and what you see as important and interesting**
- What your “major professor” or advisor studies**
- What is fundable (ugh...)**
- Participatory action research**

# Choosing an Outcome Variable

**In making your choice, be sure you can clearly answer the core question “why is this an important topic?”**

**Be careful about focusing on variables that are too general or too abstract (e.g., “adolescent risk behavior” vs. “adolescent sexual risk behavior”)**

**In making your choice, you will want to specify your target population (infants, children, adolescents, young adults, adults, the elderly)**

# Conceptual Definitions

**Whenever you introduce a variable into a model, it is important that you have a clear *conceptual definition* of that variable**

**Write out your definition in clear and unambiguous terms**

**See my theory construction book for six practical strategies for constructing clear conceptual definitions**

# **Grand versus Mid-Level Theories**

**Grand theories are broad-based frameworks that identify broad classes of variables we should think about when we want to explain a phenomenon.**

- Bronfenbrenner's ecological systems theory (individual, microsystem, mesosystem, exosystem, macrosystem)**
- Structuralism, functionalism, materialism, systems theory, symbolic interactionism, behaviorism**

**Grand theories have their place, but they typically are too general to address specific problems in ways that will yield practical, evidenced based strategies for solving problems**

# **Grand versus Mid-Level Theories**

**Mid-level theories identify specific variables that are clearly defined, that are directly tied to the outcome variable, and that elucidate specific causal mechanisms that are directly testable.**

**Most social issues require that we ultimately address them using mid-level theories**

# **The Building Blocks of Causal Theories**

# Causal Theories

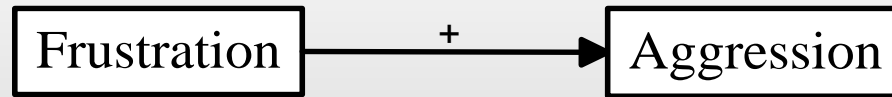
**Causal theories can be complicated, but at their core, there are six types of relationships that can be part of a causal theory**

## *Direct Causal Relationships*

**A direct causal relationship is when a variable, X, has a direct causal influence on another variable, Y:**

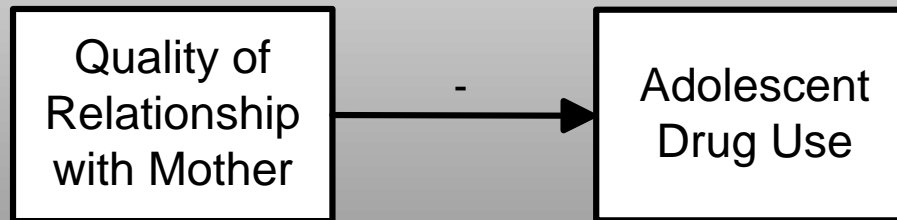
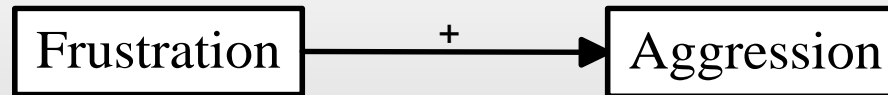


# Direct Causal Relationships





# Direct Causal Relationships



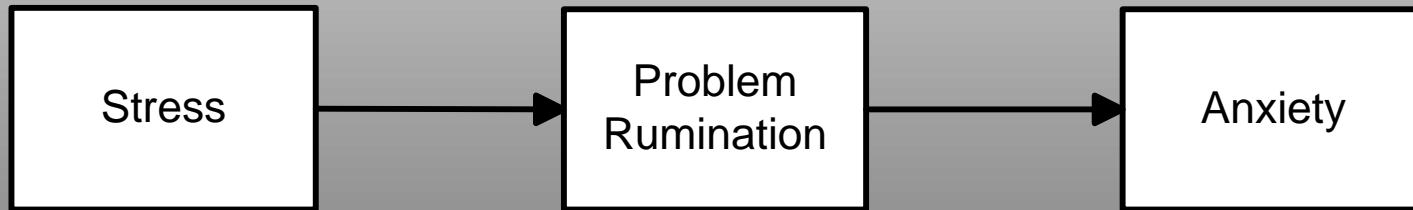
# Indirect Causal Relationships

## *Indirect Causal Relationships*

**An indirect causal relationship is when a variable, X, has a causal influence on another variable, Y, through an intermediary variable, M:**



# Indirect Causal Relationships



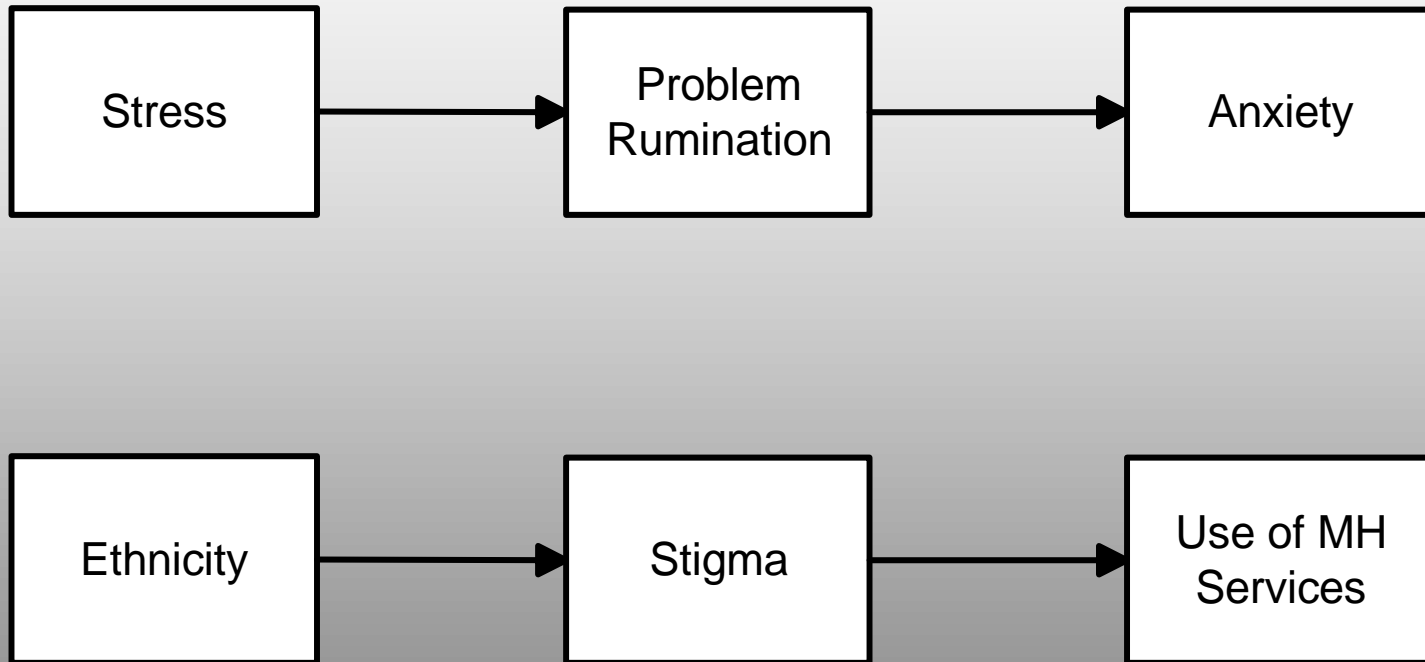
# Indirect Causal Relationships



The intermediary variable is called a *mediating variable* or a *mediator*

A mediator identifies the mechanism by which X influences Y. It answers the question “why does X influence Y”

# Indirect Causal Relationships



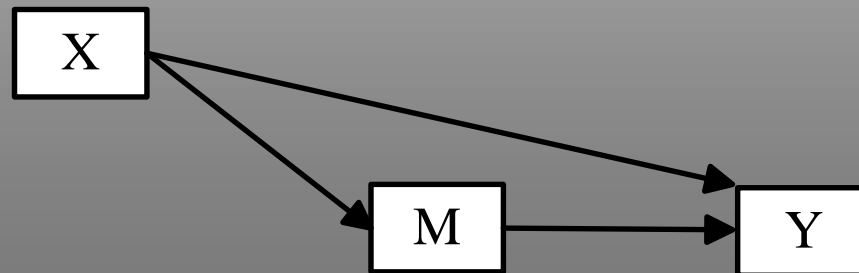
# Mediated Relationships

**Whenever you specify a mediated relationship, you must address in your theory the issue of complete versus partial mediation**

**(a) The case of complete mediation**

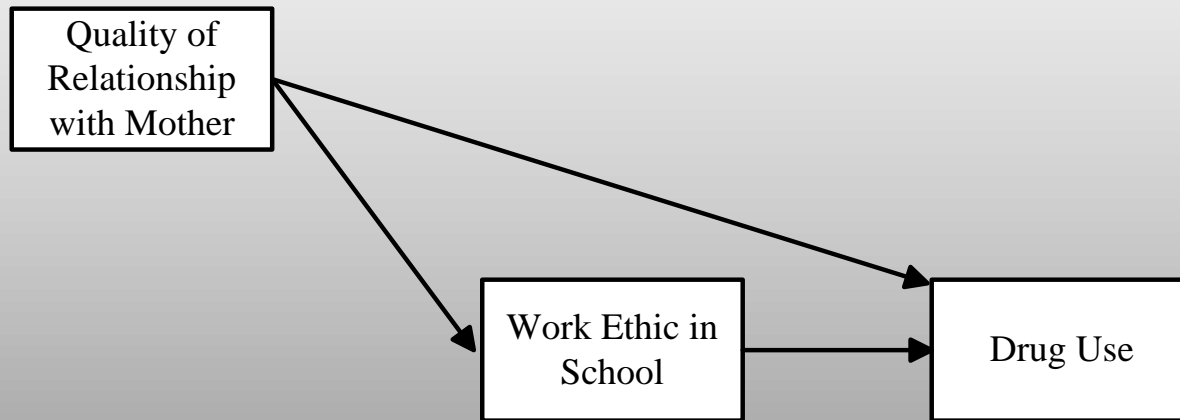


**(b) The case of partial mediation**



# Mediated Relationships

**Example of partial mediation:**

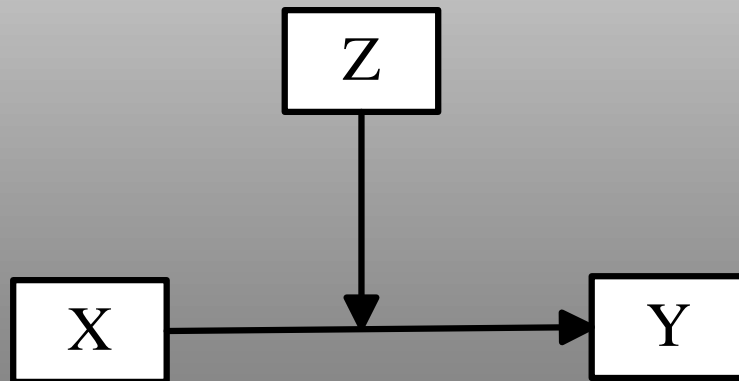


**Theoretical justification: Quality of relationship also impacts likelihood adolescent hangs out with negative peers**

# Moderated Causal Relationships

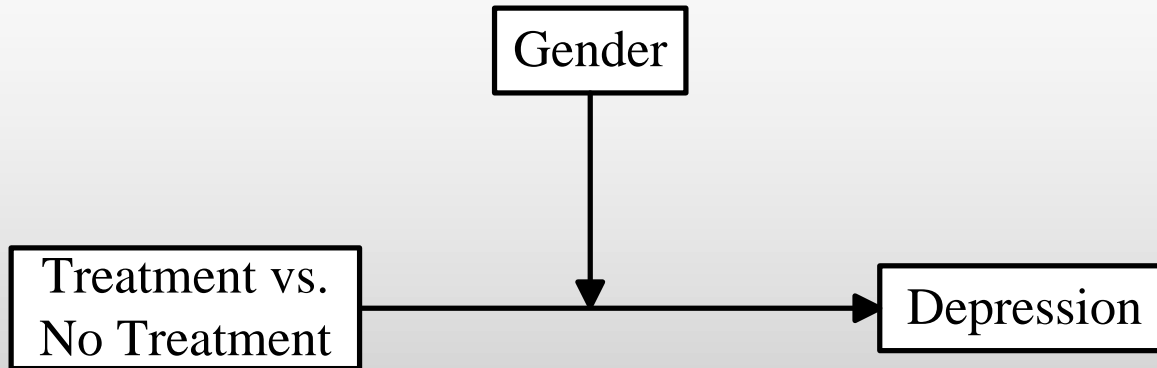
## *Moderated Causal Relationships*

A moderated causal relationship is when the *impact* of a variable, X, on another variable, Y, differs depending on the value of a third variable, Z

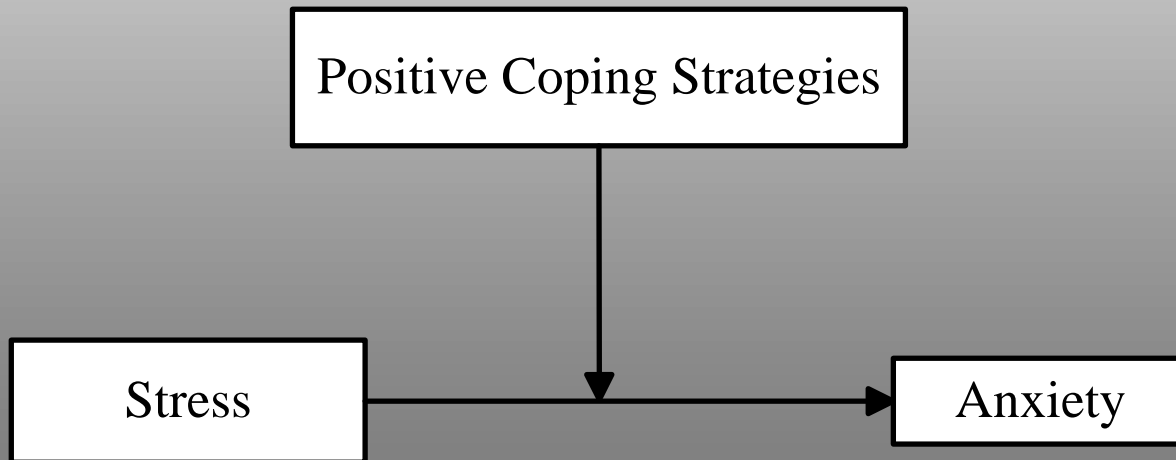
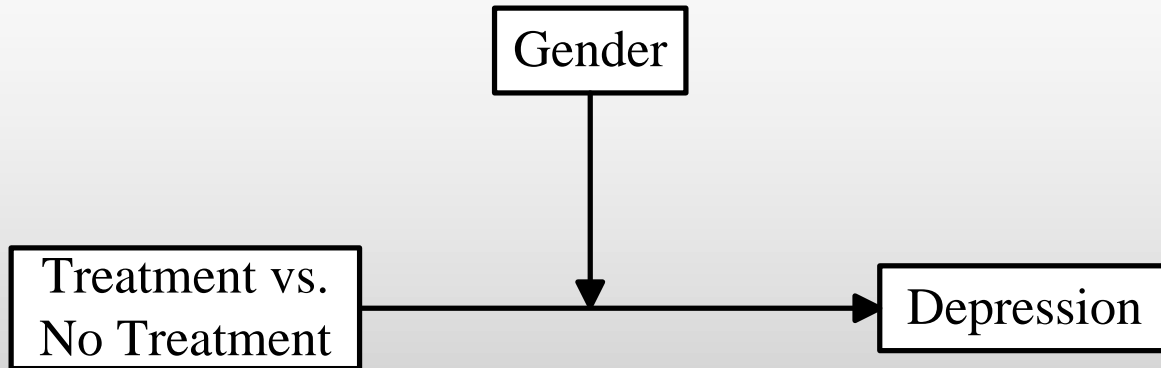




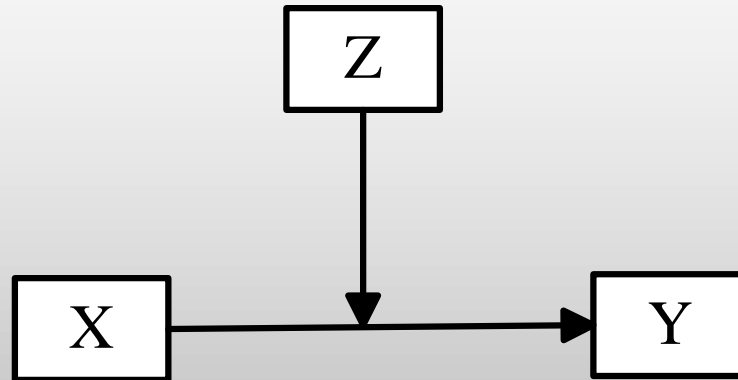
# Moderated Causal Relationships



# Moderated Causal Relationships



# Moderated Causal Relationships



The variable that “moderates” the relationship is called a *moderator* variable.

Be careful not to confuse the terminology “moderator” with “mediator.” They are very different causal dynamics!

# **Moderated Causal Relationships**

**Moderators identify subpopulations and conditions where causal relationships exist (or are stronger) versus subpopulations and conditions where they do not exist (or are weaker)**

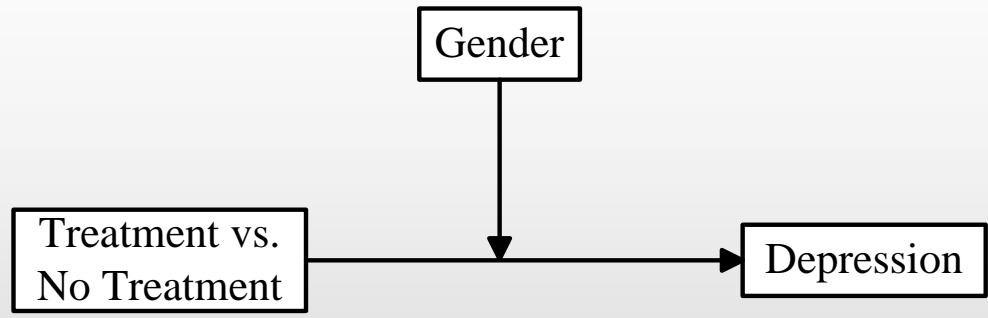
**Common moderating individual difference variables are**

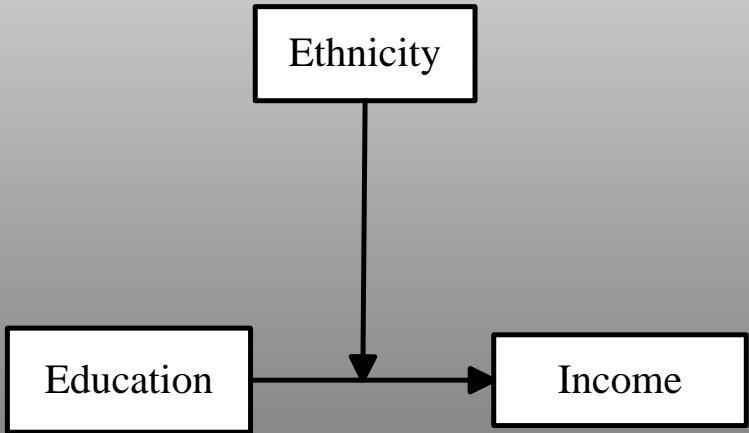
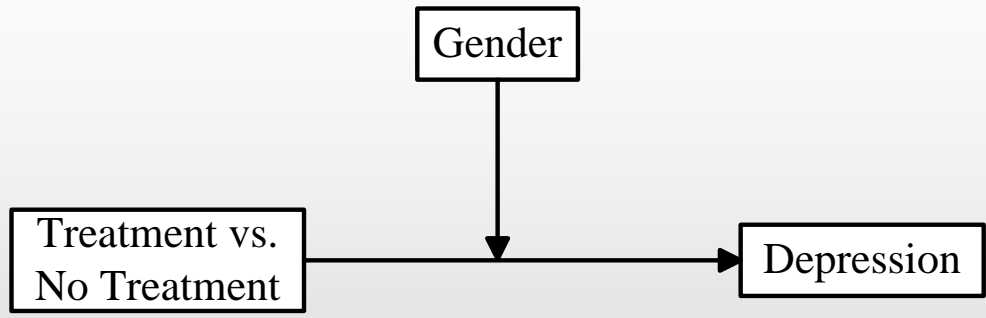
**Age/grade**

**Gender**

**Ethnicity**

**Social class**





# Moderated Causal Relationships

**Mediation asks the question *why*. Moderation asks the questions for *who*, *where* and *when***

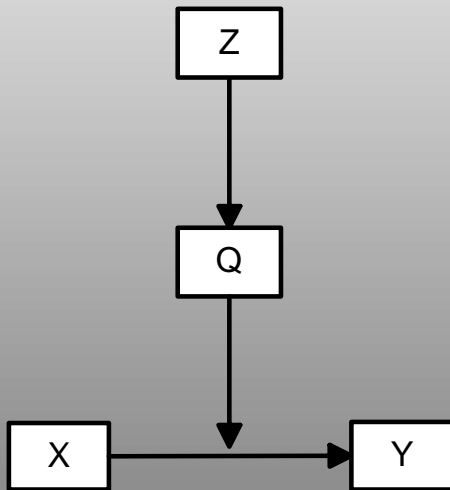
**Who? (for whom does this apply and for whom not)**

**Where? (where does this apply and where not)**

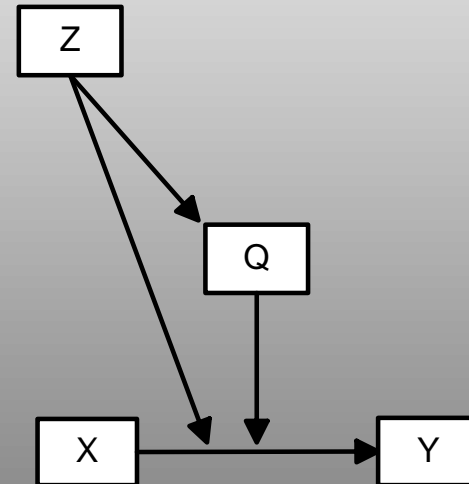
**When? (when does this apply and when not)**

# Can Combine Mediation and Moderation in Causal Models

## Mediated Moderation



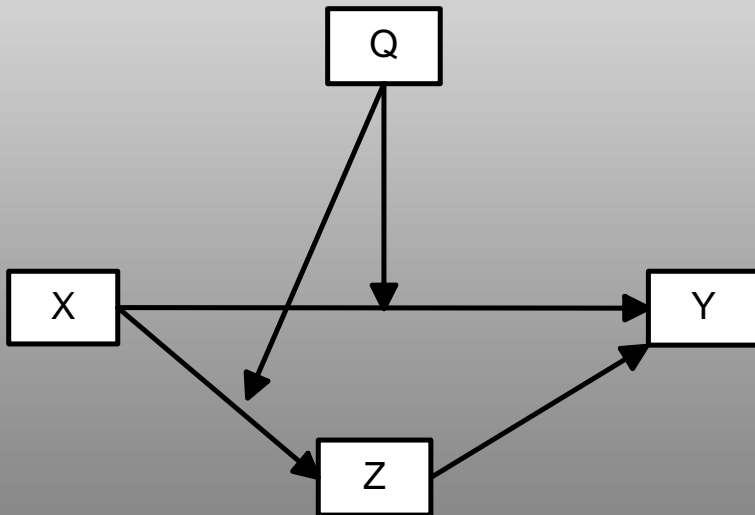
## Partial Mediated Moderation



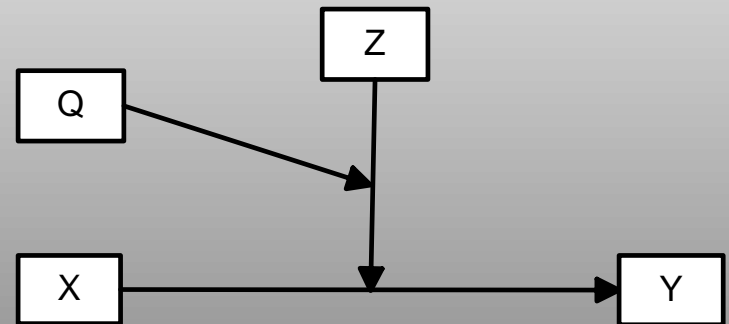


# Can Combine Mediation and Moderation in Causal Models

## Moderated Mediation



## Moderated Moderation



# Bidirectional Causal Relationships

## *Bidirectional Causal Relationships*

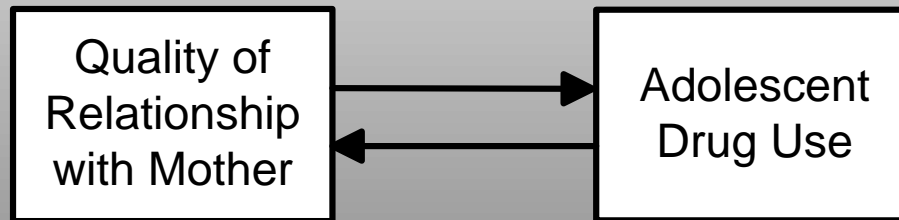
**A bidirectional causal relationship is when a variable, X, has a causal influence on another variable, Y, and that effect, Y, has a “simultaneous” impact on X:**



# Bidirectional Causal Relationships



# Bidirectional Causal Relationships

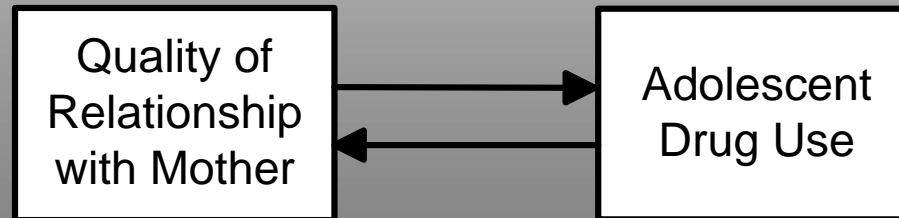


# Reciprocal Causality

**Technically, there is no such thing as reciprocal causality**

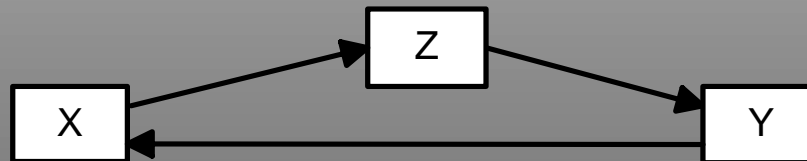
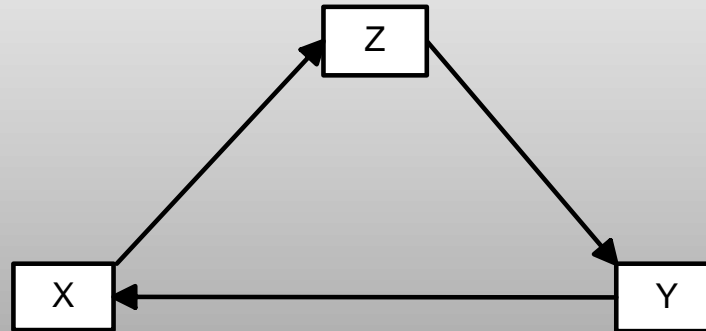


**Which translates into:**



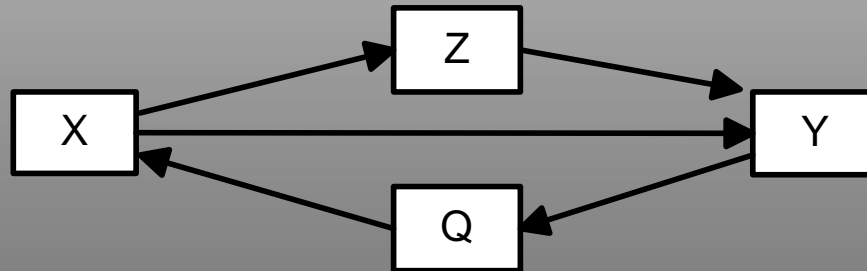
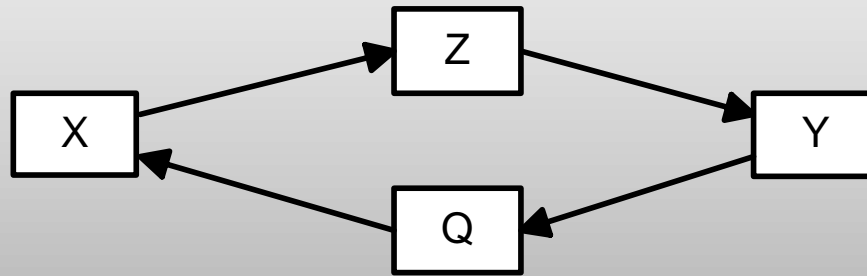
# Feedback Loops

**Feedback loops in models are simply a combination of bi-directional effects and indirect effects**



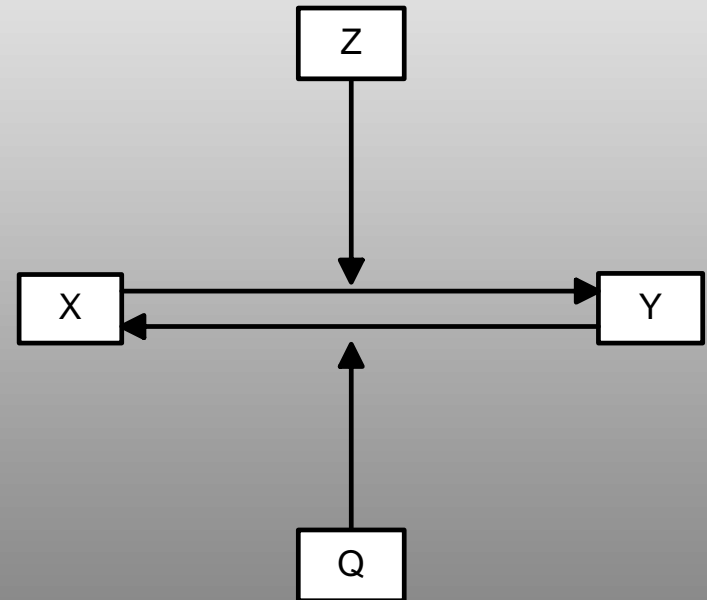
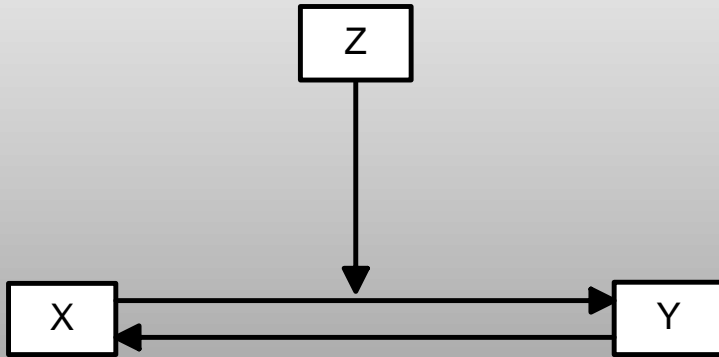
# Feedback Loops

We can have more than one mediator



# Bidirectional Causal Relationships

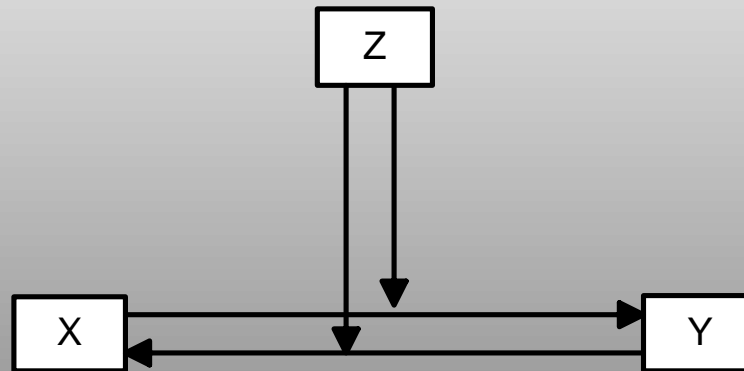
We can also add moderators





# Bidirectional Causal Relationships

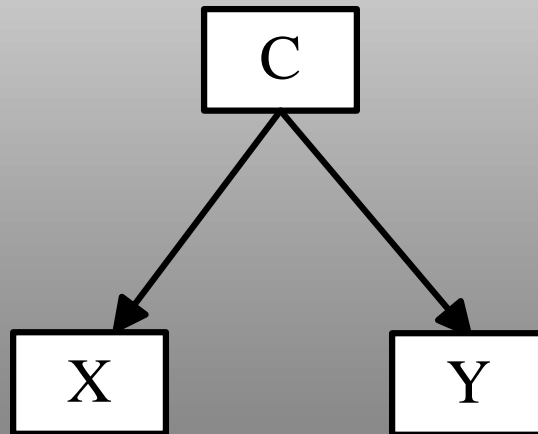
Here is an example of one moderator variable with two moderated relationships



# Spurious Relationship

## *Spurious Relationship*

***A spurious relationship is one where two variables that are not causally related share a common cause:***



# Spurious Relationship

## *Examples*

**There is a relationship between shoe size and verbal intelligence: The bigger your feet, the smarter you are!**

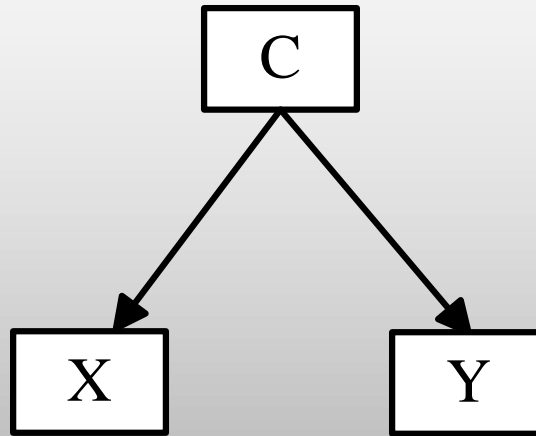
# Spurious Relationship

## *Examples*

**There is a relationship between shoe size and verbal intelligence: The bigger your feet, the smarter you are!**

**There is a relationship between how long your hair is and how tall you are: The shorter your hair, the taller you grow!**

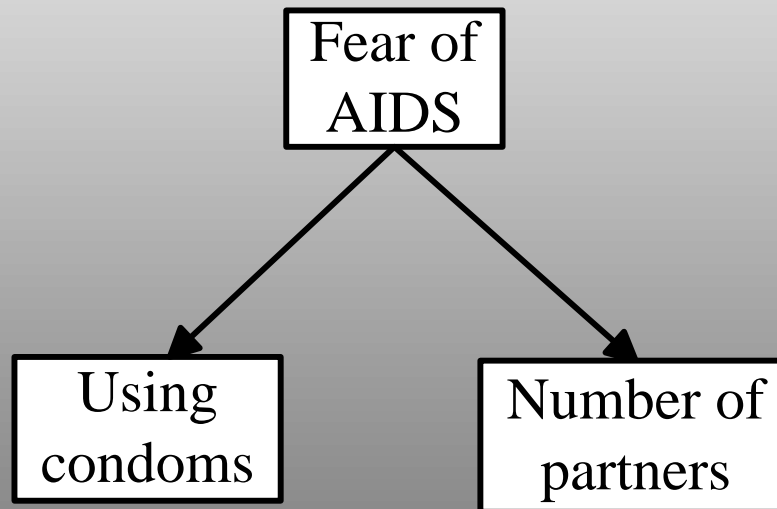
# Spurious Relationship



The common cause is called a *confound*, but this term is used to characterize other scenarios in the social sciences as well

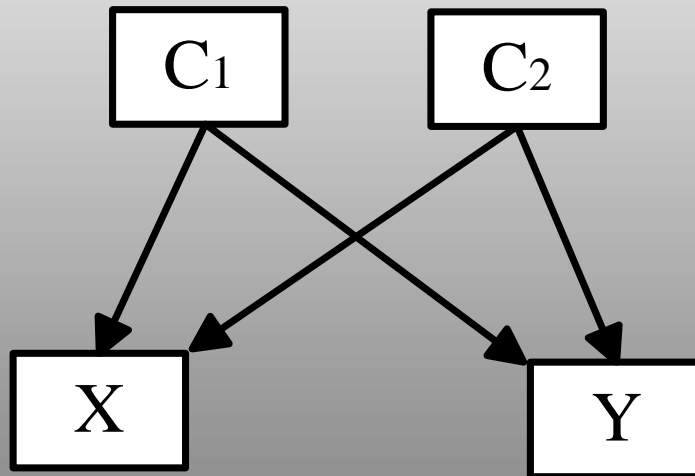
# Spurious Relationship

**Spurious relationships are not necessarily “bad” or misleading. They can be conceptually meaningful**



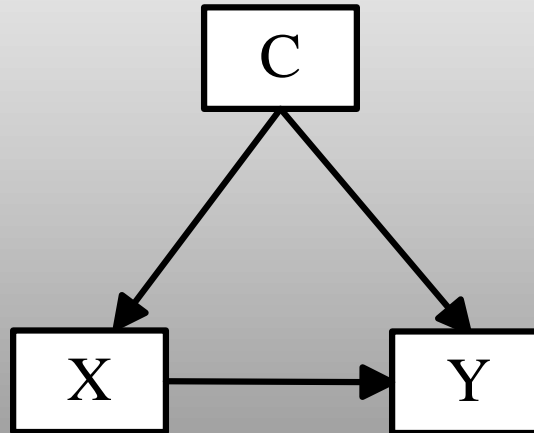
# Spurious Relationship

**There can be more than one confound in a model:**



# Spurious Relationship

Relationships can be *both* causal and spurious





# Unanalyzed Relationships

## *Unanalyzed Relationships*

**An unanalyzed relationship is one where the possibility of two variables being correlated is acknowledged, but there is no interest in describing the causal dynamics between the variables, if there are any. The relationship will remain “unanalyzed.”**



# **Summary of Core Relationships**

**Direct causal relations**

**Indirect (mediated) causal relations**

**Moderated causal relations**

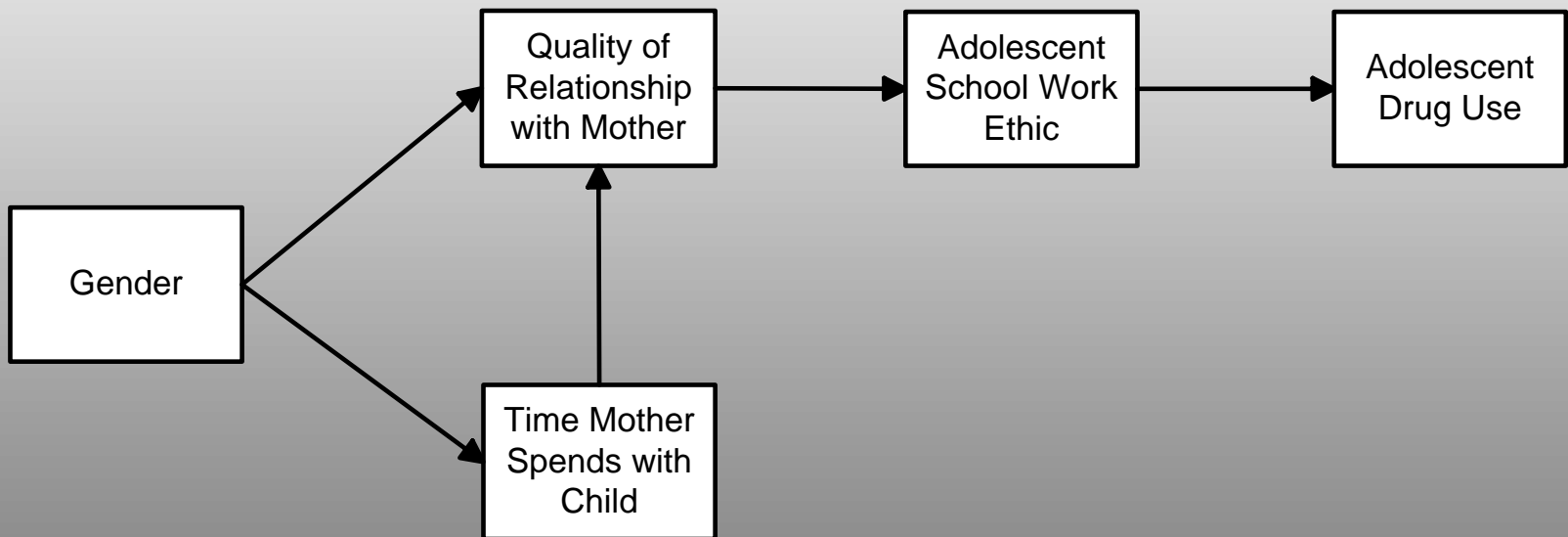
**Bidirectional causal relations**

**Spurious relations**

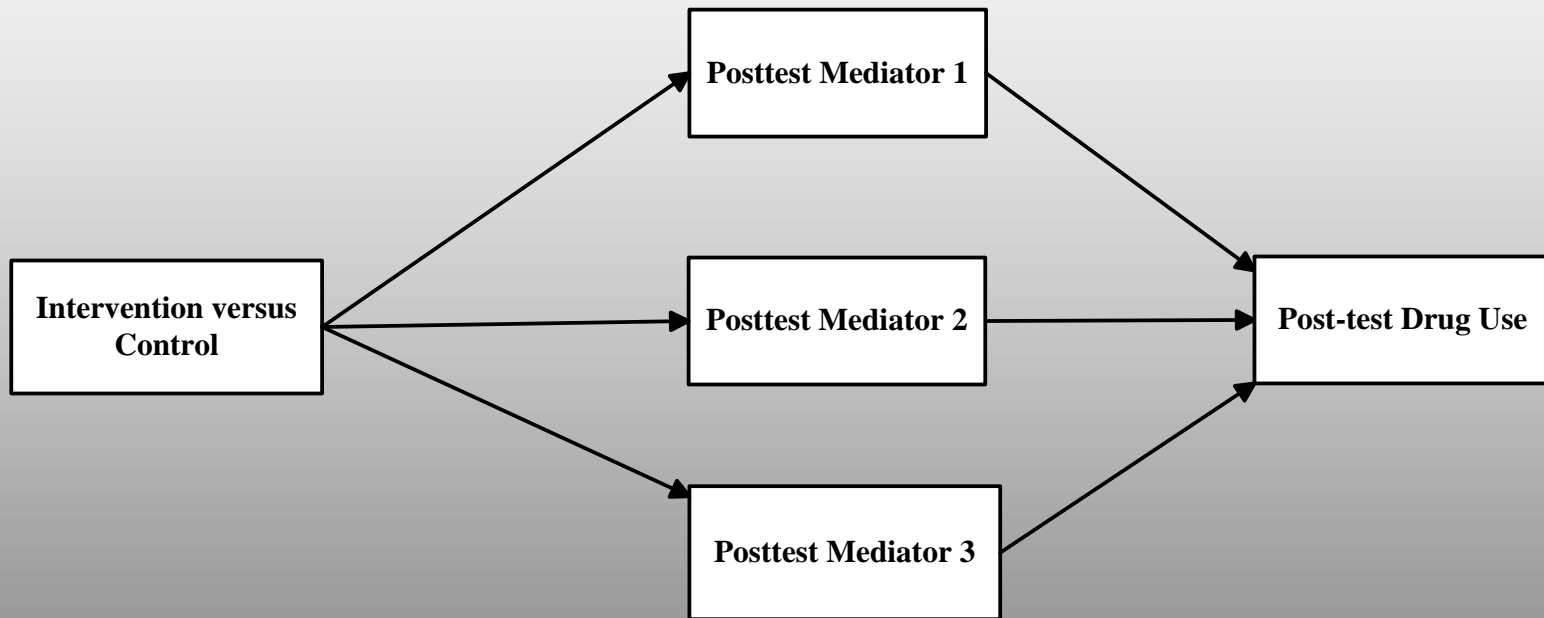
**Unanalyzed relations**

# Causal Theories

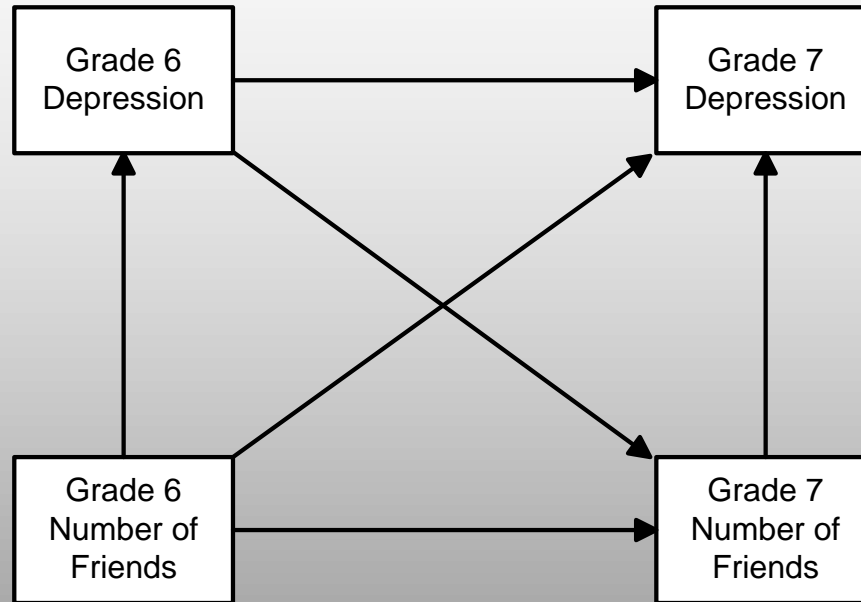
**We put all these ideas together to build complex theories of phenomena. Here is one example:**



# An Intervention With Three Mediators

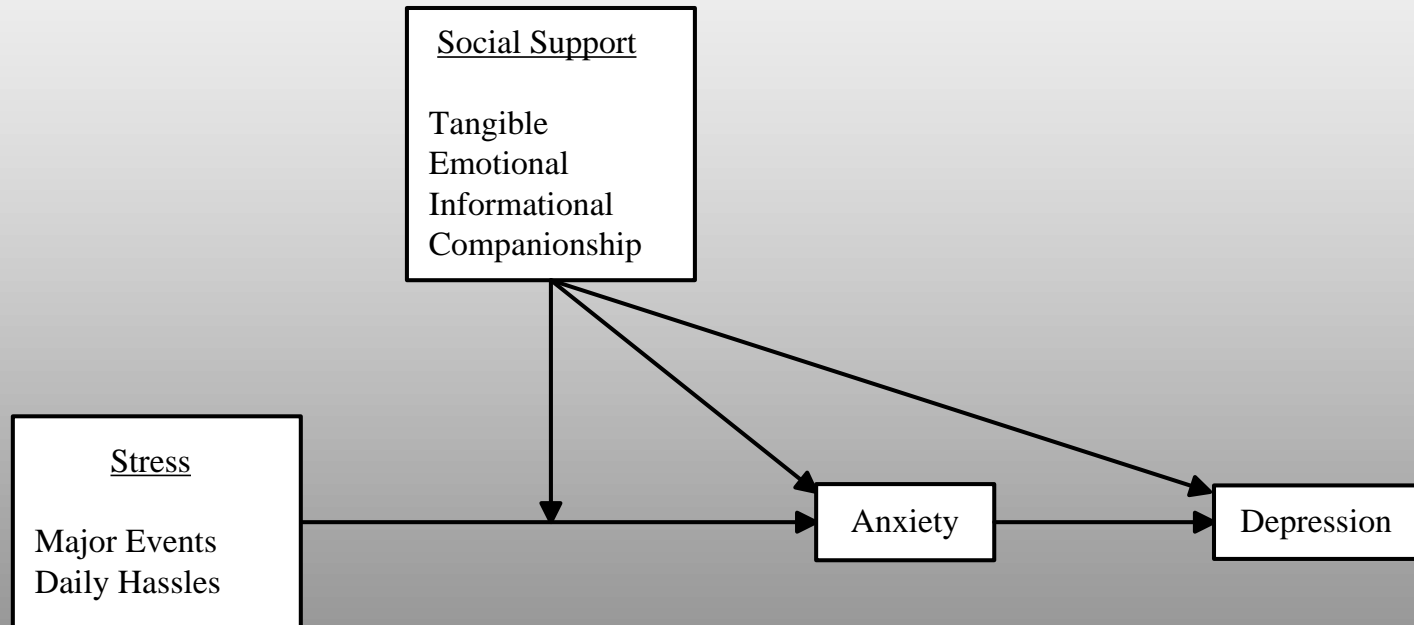


# A Longitudinal Model



**This model has autoregressive effects, contemporaneous effects, and lag effects**

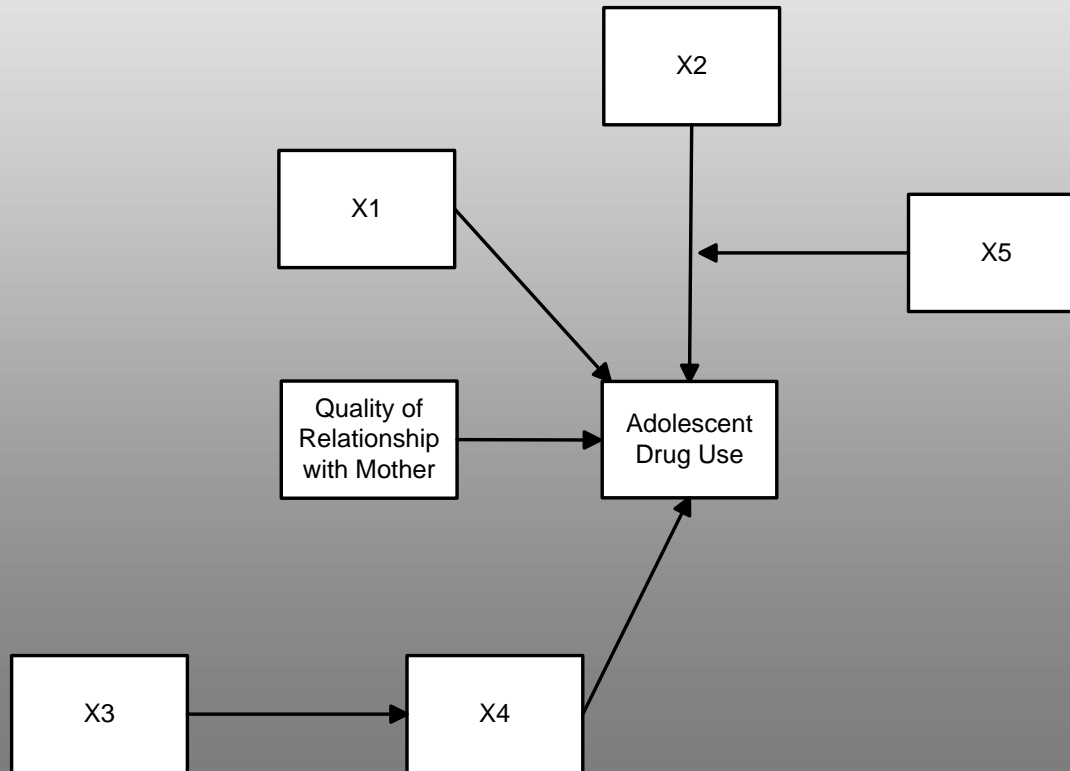
# Portraying Complex Models



# **Building Your Own Original Theory**

# Building Your Theory

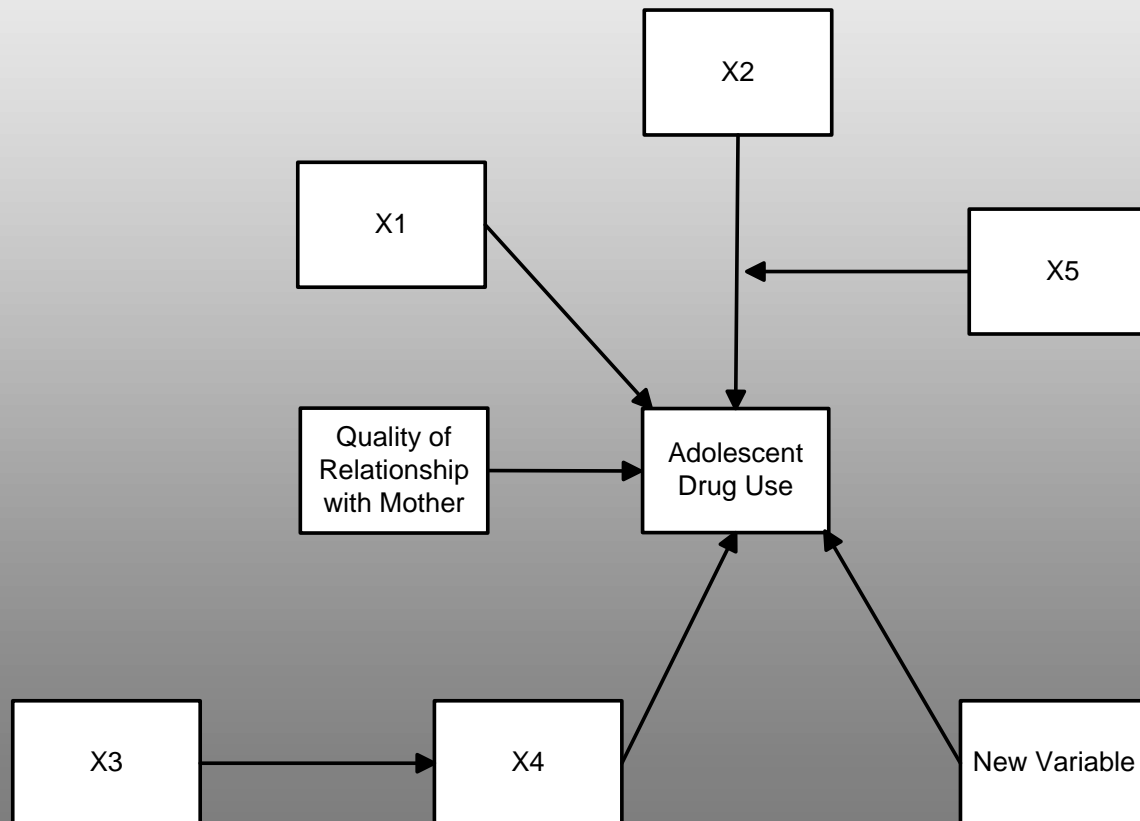
**After identifying your outcome, read the extant literature on it and draw an influence diagram that captures what the current “state of knowledge” has to say:**





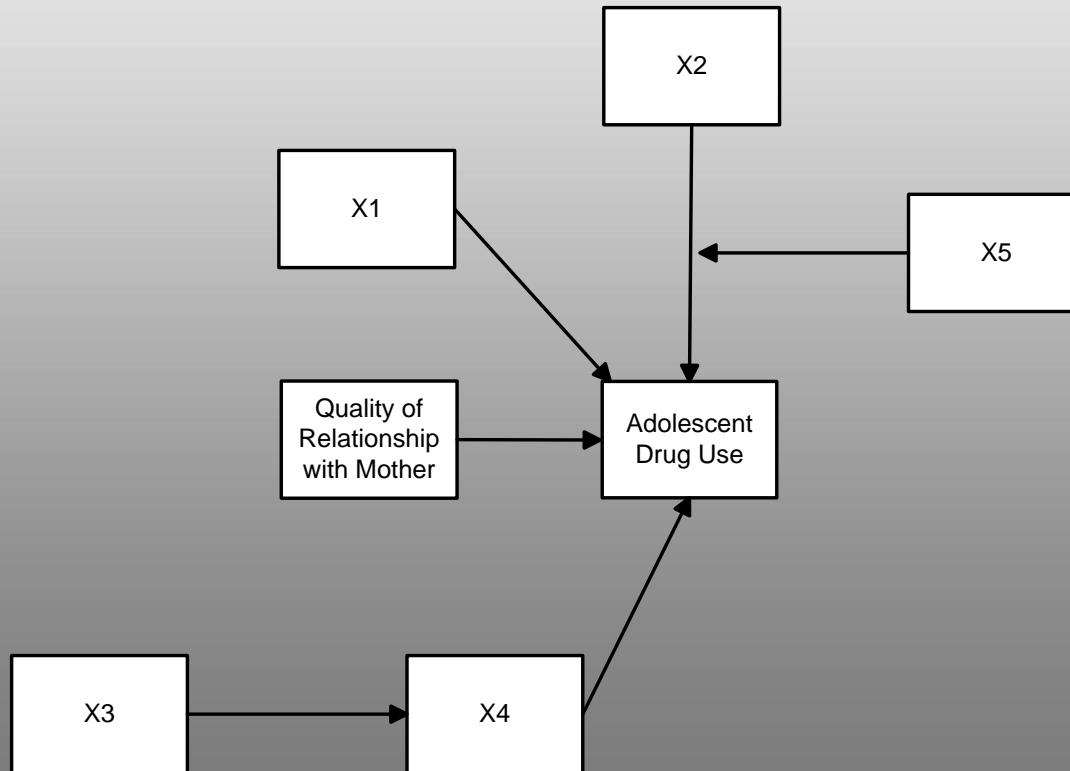
# Building Your Theory

**If you think of a new variable that the literature has ignored, then add it to the system; that is a theoretical contribution!**



# Building Your Theory

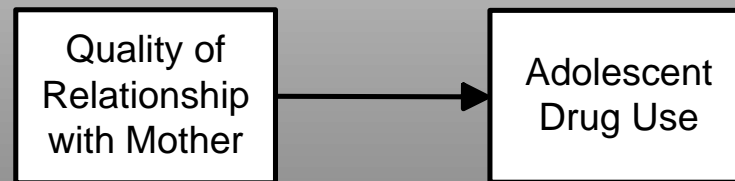
**Or, take an existing relationship and expand on it in novel ways to expand and strengthen the theory**



# Building Your Theory by Adding Mediation

**Consider turning the direct relationships into an indirect relationship**

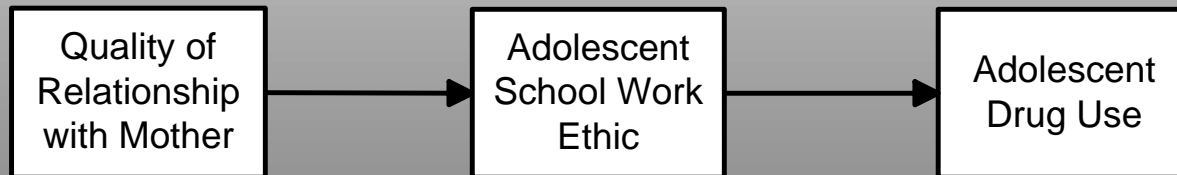
**There are three strategies for turning a direct relationship into an indirect or mediated relationship**



# Building Your Theory by Adding Mediation

**Strategy 1: Use the *why heuristic*. i.e. state *why* one variable influences the other variable. The articulation will reveal the mediator**

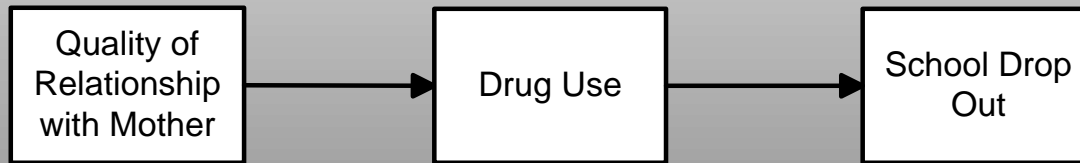
**Example: Why does a poor relationship with parents lead to drug use?**



# Building Your Theory by Adding Mediation

**Strategy 2: *Identify an effect of an effect.* Think of your outcome variable as a direct cause of another variable**

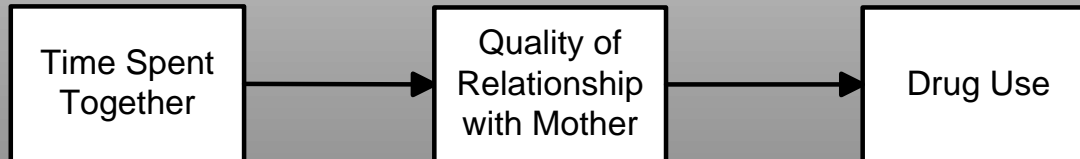
**Example: Drug use leads to dropping out of school**



# Building Your Theory by Adding Mediation

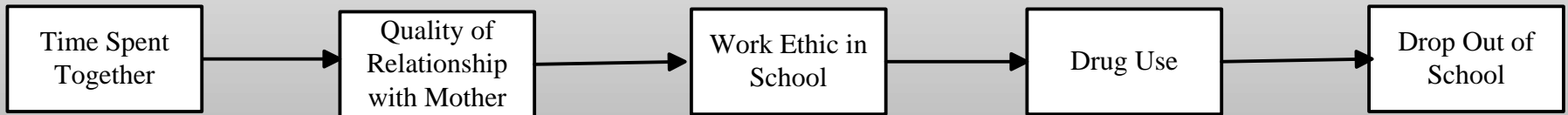
**Strategy 3: *Identify a cause of a cause.* Think of your cause as an outcome variable and identify a direct cause of it**

**Example: Time mother and child spend together affects the quality of the relationship with the mother**



# Building Your Theory by Adding Mediation

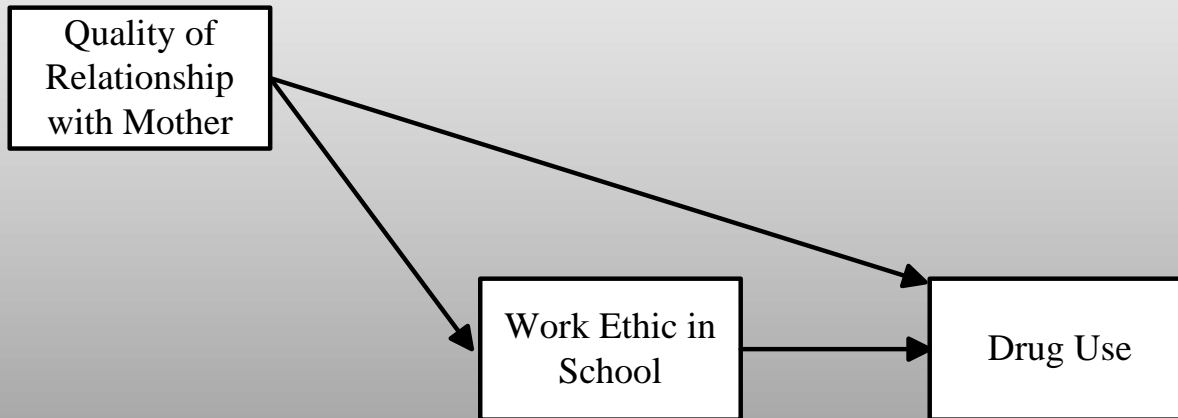
**We often end up with mediated relationships with multiple links in the mediational chain**



**We are interested in “new” relationships within the chain that represent theoretical innovations**

# Building Your Theory by Adding Mediation

**For each mediated relationship, specify if there is partial or complete mediation:**

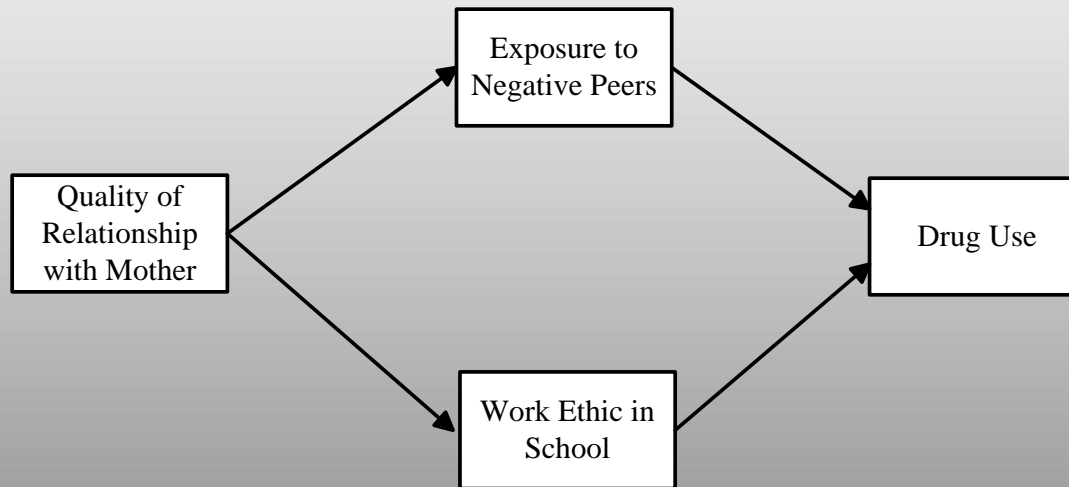


**Theoretical justification: Quality of relationship also impacts likelihood adolescent hangs out with negative peers**



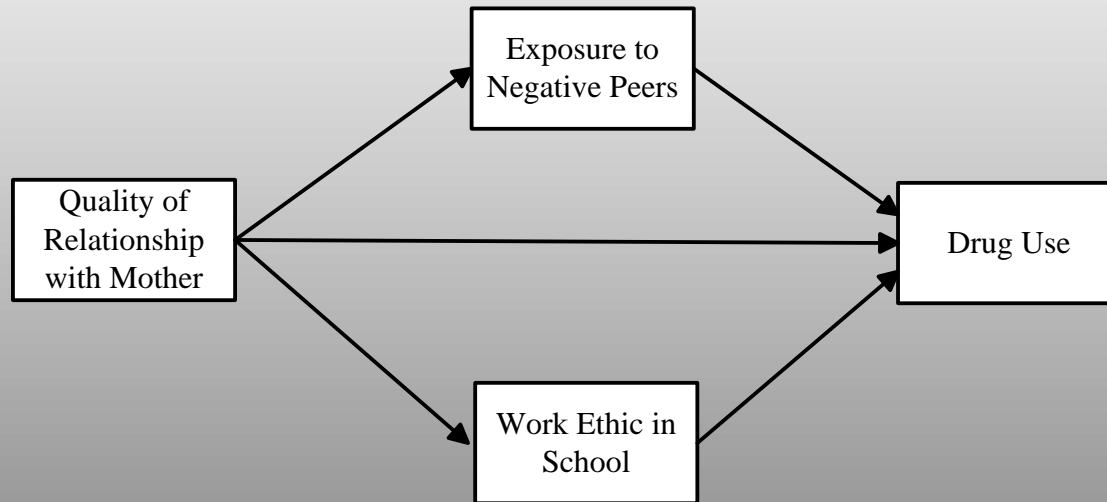
# Building Your Theory by Adding Mediation

**Why not:**



# Building Your Theory by Adding Mediation

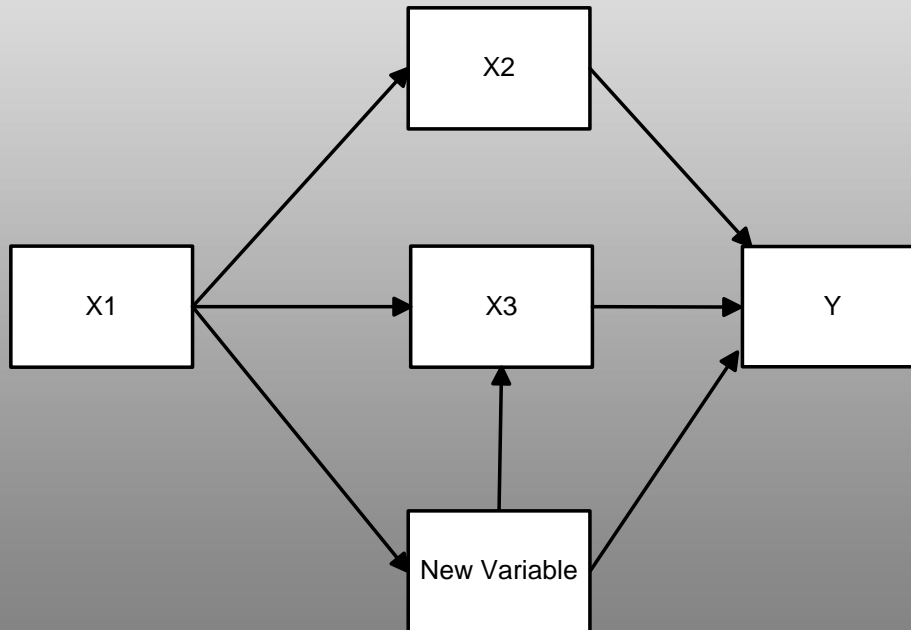
Can do so, but then must address issues of partial versus complete mediation for these mediators:



The process is never-ending. At some point, we need to close out the system

# Building Your Theory by Adding Mediation

Maybe the literature has identified two mediators, but you think of a mediator that no one has considered. This is a theoretical contribution – a new mechanism



# **Build Your Theory by Adding Bidirectional Effects**

**Consider turning the direct relationships into a reciprocal causal effect**

**Ask yourself if it is feasible for the causal direction to go the other way**

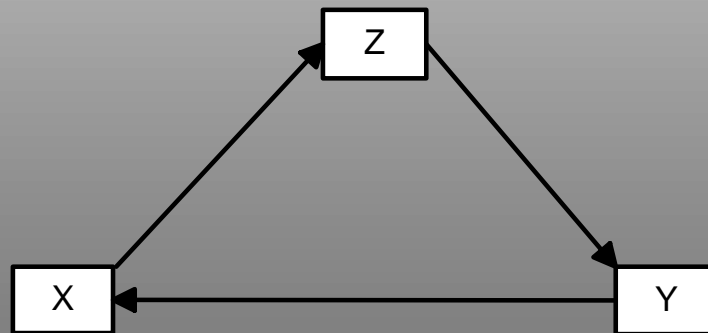
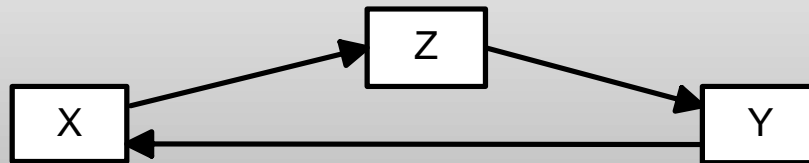
**Gender impacts depression**

**Religiosity impacts adolescent sexual behavior**

**Childhood trauma impacts adolescent depression**

# Build Your Theory by Adding Bidirectional Effects

Consider turning the bidirectional relationship into a feedback loop by adding a mediator to it



# **Build Your Theory by Adding Moderated Effects**

**Pick a direct relationship to focus on and then try to identify a moderator of it**

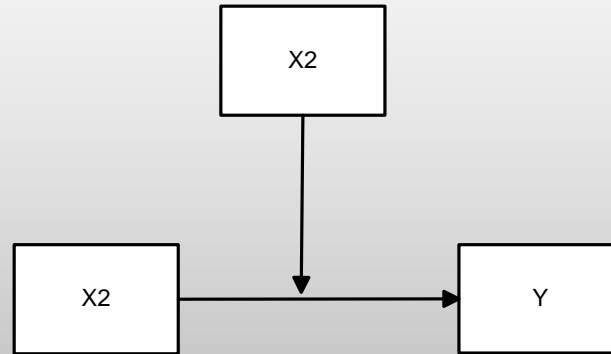
**To identify moderators, ask the questions and their negations:**

**Who? (for whom does this apply and for whom not)**

**Where? (where does this apply and where not)**

**When? (when does this apply and when not)**

# Build Your Theory by Adding Moderated Effects



**After doing so, consider adding mediated moderation, moderated moderation, or moderated mediation**

# **Common Mistakes**

**Model is too complex – too many variables**

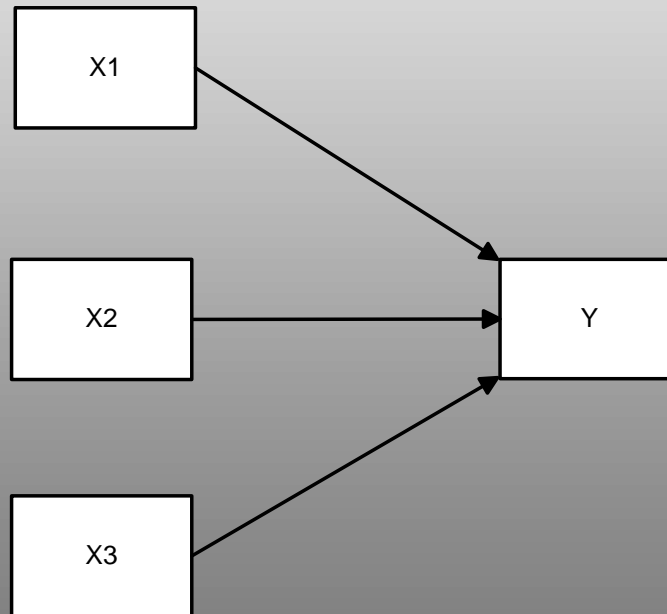
**Variables are not clearly defined**

**Variables are too abstract and too general**



# Common Mistakes

**Know that when you run a single equation model (one regression equation, one logistic equation, one survival analysis), the model you are assuming is this:**



Theory  
Construction and  
Model-Building  
Skills



A Practical Guide for Social Scientists

James Jaccard | Jacob Jacoby

# **Analyzing Causal Models**

# Analyzing Causal Models

**Most people associate causal modeling with *structural equation modeling* (SEM; also called *path analysis*)**

**There are two general forms of SEM analysis, *limited information estimation* and *full information estimation*. Most people are familiar with just the latter**

**Each has strengths and weaknesses. I will be showing you limited information estimation.**

# Analyzing Causal Models

**When social scientists address causal models, they rely heavily on the linear model, a mathematical function that describes the relationship between two variables**

**The model is usually applied when characterizing the relationship between two continuous variables, but as we will see, it can be adapted to model a wide range of variable types**

**We will be using multiple regression analysis, so I want to briefly review it with you.**

# **Multiple Regression Analysis**

# The Linear Model

The general form of the linear model is

$$Y = \alpha + \beta X + \varepsilon$$

or, using sample notation,

$$Y = a + B X + e$$

If I think annual income is a linear function of the number of years of education people have, I would write the equation

$$\text{Income} = \alpha + \beta \text{Education} + \varepsilon$$

# The Linear Model

$$\text{Income} = \alpha + \beta \text{ Education} + \varepsilon$$

There are three key parameters in the linear model

$\alpha$  = the intercept

$\beta$  = the regression coefficient or the slope

$\varepsilon$  = the error term, the residual term, or the disturbance term

Each parameter has a numerical value associated with it that is subject to meaningful interpretation



# The Linear Model

$$\text{Income} = \alpha + \beta \text{ Education} + \varepsilon$$

**Suppose that I collect data on annual income and the number of years of education of people and analyze the data using the SPSS regression package. I might observe the following regression equation:**

$$\text{Income} = 10,000 + 2,000 \beta + e$$

**What do these numbers mean?**

# The Linear Model

$$Y = a + B X + e$$

$$\text{Income} = 10,000 + 2,000 \beta + e$$

$a$  is the predicted mean on  $Y$  when  $X = 0$ . In this case, it is 10,000.

Intercepts are useful but they are rarely interpreted in social science research. I am not going to spend much time on them in this workshop

# The Linear Model

| <u>Education</u> | <u>Mean Income</u> | <u>SD of Income</u> |
|------------------|--------------------|---------------------|
| 8                | 26,000             | 5,000               |
| 9                | 28,000             | 5,000               |
| 10               | 30,000             | 5,000               |
| 11               | 32,000             | 5,000               |
| 12               | 34,000             | 5,000               |

$$Y = a + B X + e$$

$$\text{Income} = 10,000 + 2,000 \text{ Education} + e$$

**B** tells us for every one unit that **X** increases, how much the mean on **Y** is predicted to change

# The Linear Model

$$Y = \alpha + \beta X + \varepsilon$$

$$\text{Income} = \alpha + \beta \text{Education} + \varepsilon$$

The  $\varepsilon$  represent factors other than  $X$  that impact  $Y$ . They are often called residuals, errors, or disturbances.

The magnitude of the disturbances is often represented as  $1$  minus the squared correlation between  $X$  and  $Y$ .

# The Linear Model

$$Y = \alpha + \beta X + \varepsilon$$

$$\text{Income} = \alpha + \beta \text{Education} + \varepsilon$$

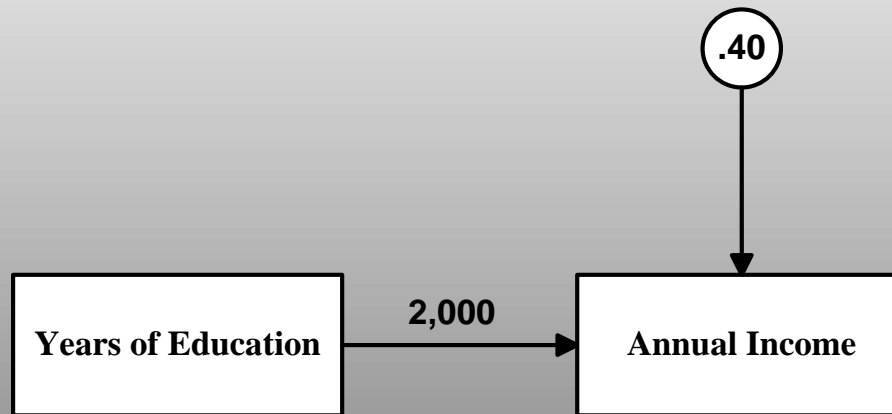
If I tell you the “disturbance value” is 0.30, then this means that X accounts for 70% of the variance in Y and 30% is due to other factors (or is “unexplained”).

If I tell you the “disturbance value” is 0.80, then this means that X accounts for 20% of the variance in Y and 80% is due to other factors.

(terminology of eta squared)

# The Linear Model

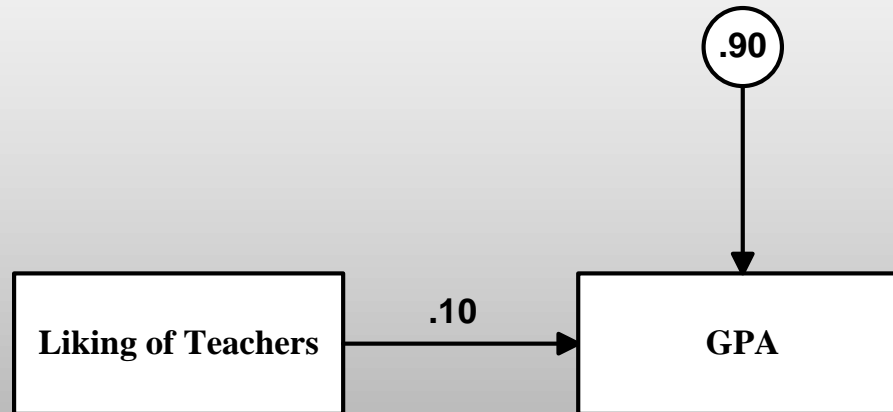
I can represent the key results of the linear analysis as applied to a set of data using path diagrams in the framework of causal modeling and it would look like this:



(note the absence of the intercept term)

# The Linear Model

Here is another example:

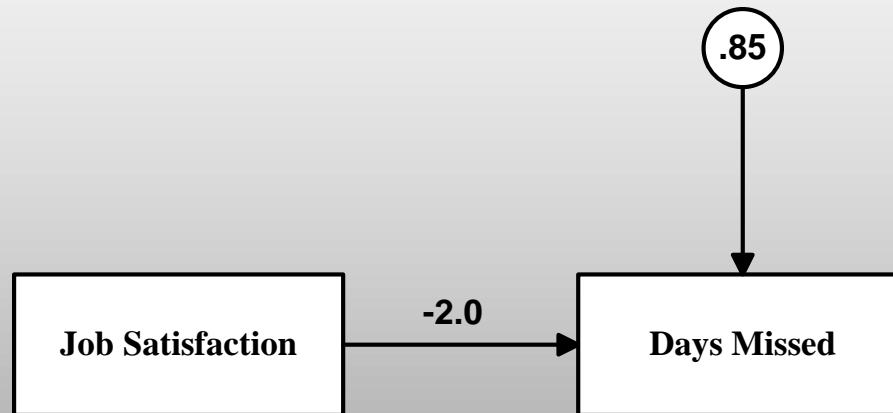


In general, how much do you like your teachers in your school?

- 1 = Very much dislike them
- 2 = Moderately dislike them
- 3 = Neither
- 4 = Moderately like them
- 5 = Very much like them

# The Linear Model

And yet another example:



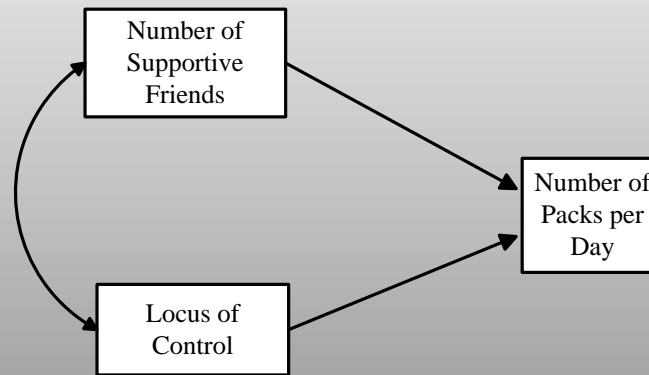
How satisfied are you with your job and the work you do for your job?

- 1 = Very dissatisfied
- 2 = Moderately dissatisfied
- 3 = Neither
- 4 = Moderately satisfied
- 5 = Very satisfied



# Multiple Regression

We can expand the analysis to include multiple determinants or “predictors,” and this is called *multiple regression analysis*



$$\text{Packs} = \alpha + \beta_1 \text{Friends} + \beta_2 \text{Control} + \varepsilon$$

$$Y = \alpha + \beta_1 X + \beta_2 Z + \varepsilon$$

# Multiple Regression

$$\text{Packs} = \alpha + \beta_1 \text{Friends} + \beta_2 \text{Control} + \varepsilon$$

Suppose that I collect data on smoking, the number of supportive friends and locus of control and analyze the data using the SPSS regression package. I might observe the following regression equation:

$$\text{Packs} = 1.0 + -0.20 \text{Friends} + -0.10 \text{Control} + \varepsilon$$

What do these numbers mean?

# Multiple Regression

$$\text{Packs} = \alpha + \beta_1 \text{Friends} + \beta_2 \text{Control} + \varepsilon$$

$$\text{Packs} = 1.0 + -0.20 \text{Friends} + -0.10 \text{Control} + \varepsilon$$

A regression coefficient is the number of units that the mean of Y is predicted to change, given a one unit increase in the target predictor, *holding all other predictors constant*

# Multiple Regression

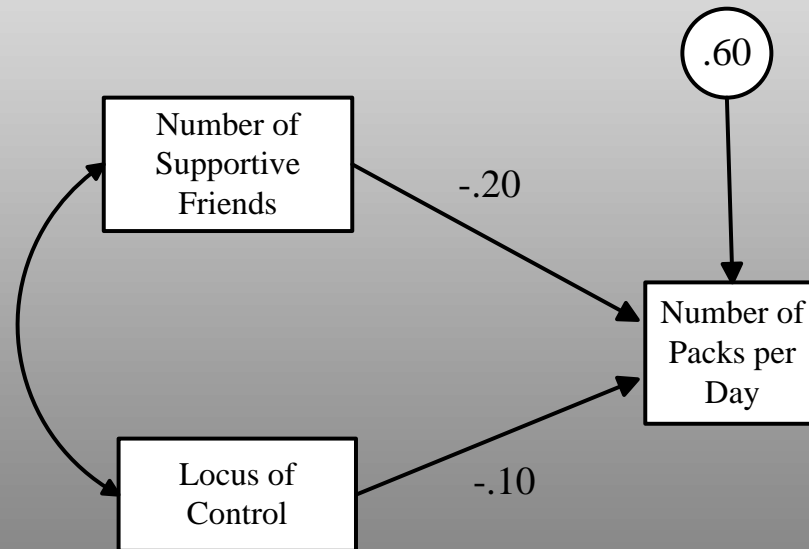
$$\text{Packs} = \alpha + \beta_1 \text{Friends} + \beta_2 \text{Control} + \varepsilon$$

$$\text{Packs} = 1.0 + -0.20 \text{Friends} + -0.10 \text{Control} + \varepsilon$$

**R squared or eta squared is the proportion of variability in Y that all predictors, considered simultaneously, account for. The 'disturbance value' is the proportion of unexplained variance in Y**

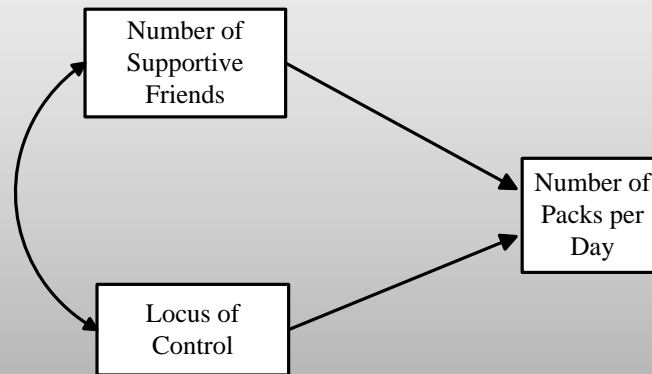
# Multiple Regression

I can represent the key results of the linear analysis as applied to a set of data using path diagrams in the framework of causal modeling and it would look like this:



# Representing Causal Models as Equations

There is a key concept I am using here. I draw my causal model:

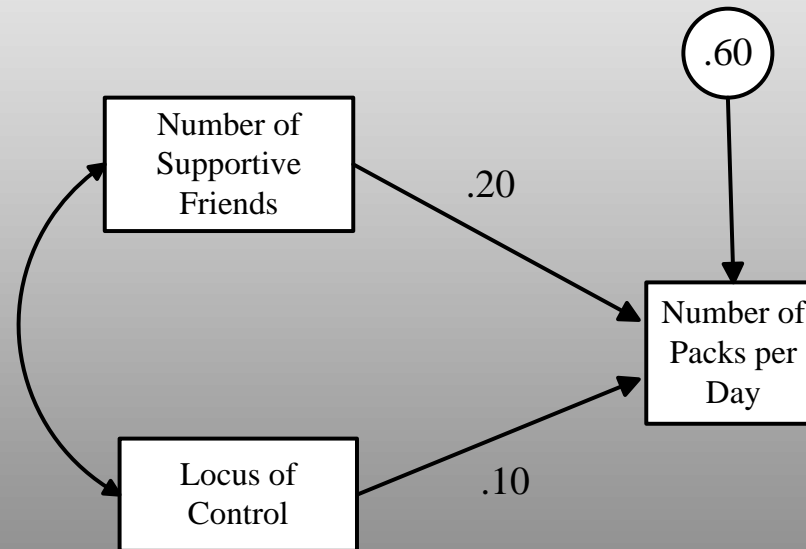


I then represent it as a “multiple regression” problem (i.e., as a linear equation):

$$\text{Packs} = \alpha + \beta_1 \text{Friends} + \beta_2 \text{Control} + \varepsilon$$

# Representing Causal Models as Equations

Then I use SPSS or SAS to estimate key coefficients in the model using standard multiple regression methods:



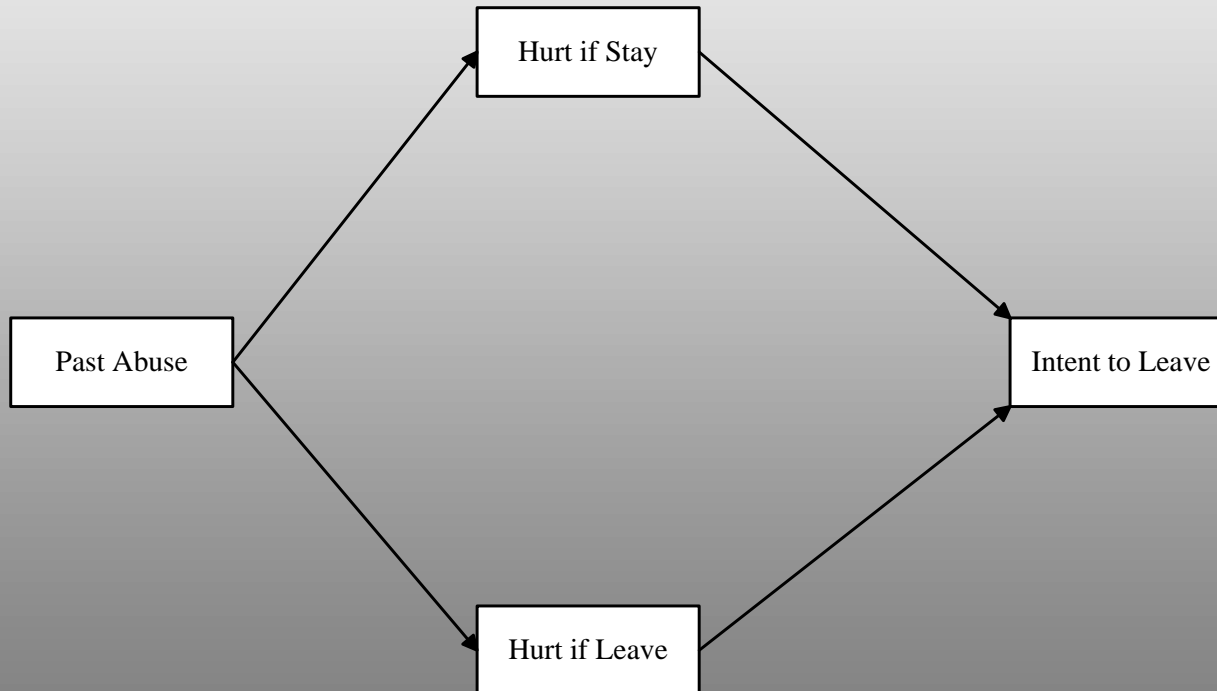
and interpret the coefficients accordingly

# **Limited Information SEM**



# Limited Information SEM

To analyze a causal model, we first draw a path diagram of that model:



# Abuse Example

## *Intention to leave relationship in the next 3 months*

**I intend to leave this relationship in the next 3 months**

**1 = strongly disagree**

**2 = moderately disagree**

**3 = neither**

**4 = moderately agree**

**5 = strongly agree**

## *Physically hurt if try to leave*

**If I try to leave the relationship in the next 3 months, he will physically hurt me**

**1 = strongly disagree**

**2 = moderately disagree**

**3 = neither**

**4 = moderately agree**

**5 = strongly agree**

# Abuse Example

## Physically hurt if stay

**If I stay in this relationship for the next 3 months, he will probably physically hurt me**

**1 = strongly disagree**

**2 = moderately disagree**

**3 = neither**

**4 = moderately agree**

**5 = strongly agree**

## Past Abuse

**How many times over the past 3 months has he physically hurt you?**

**\_\_\_\_\_ number of times**

# Abuse Example

**We identify endogenous and exogenous variables in the system.**

***Endogenous variable* is any variable with a causal arrow going to it**

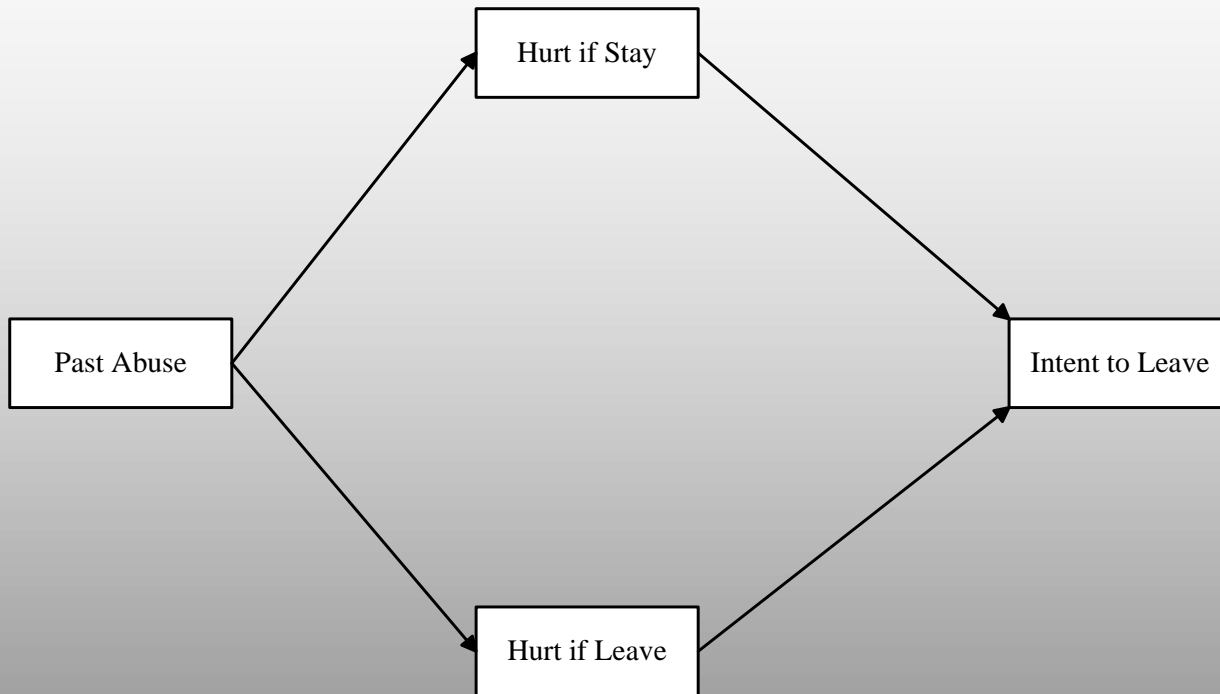
***Exogenous variable* is any variable with no causal arrow going to it**

**Next, we translate the model into a set of linear equations**

**There is one equation for each endogenous variable**

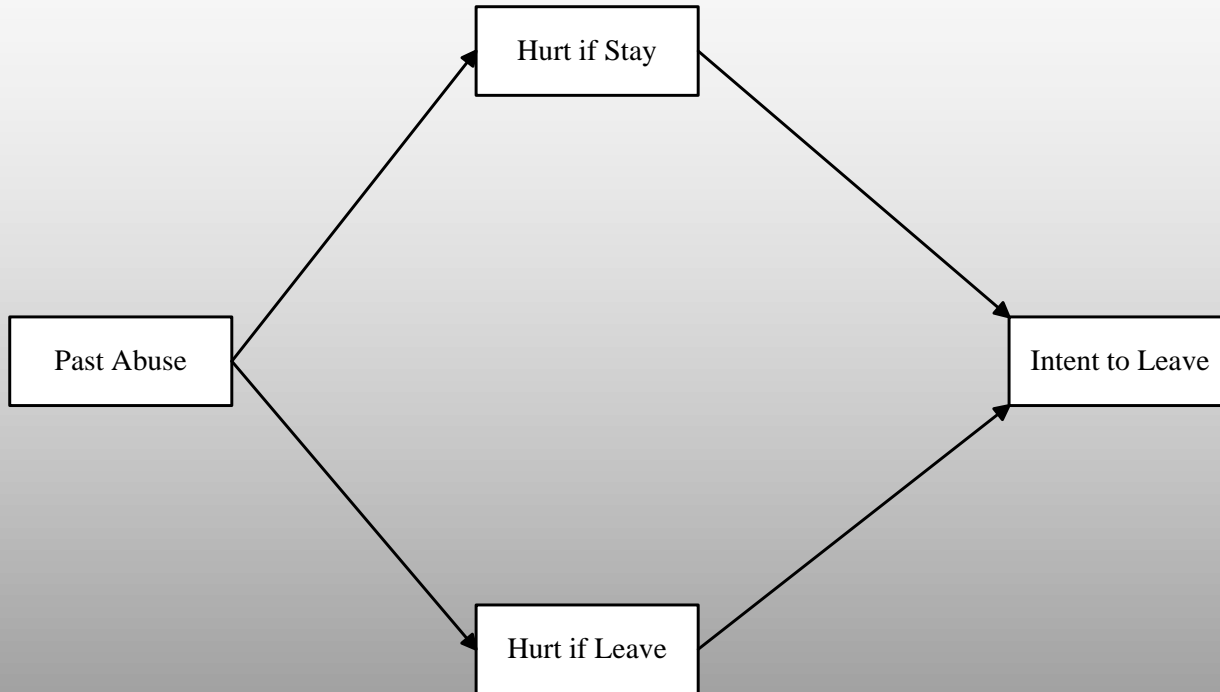
**The Y variable is the endogenous variable. The Xs are all variables that have an arrow going directly to Y**

# Abuse Example



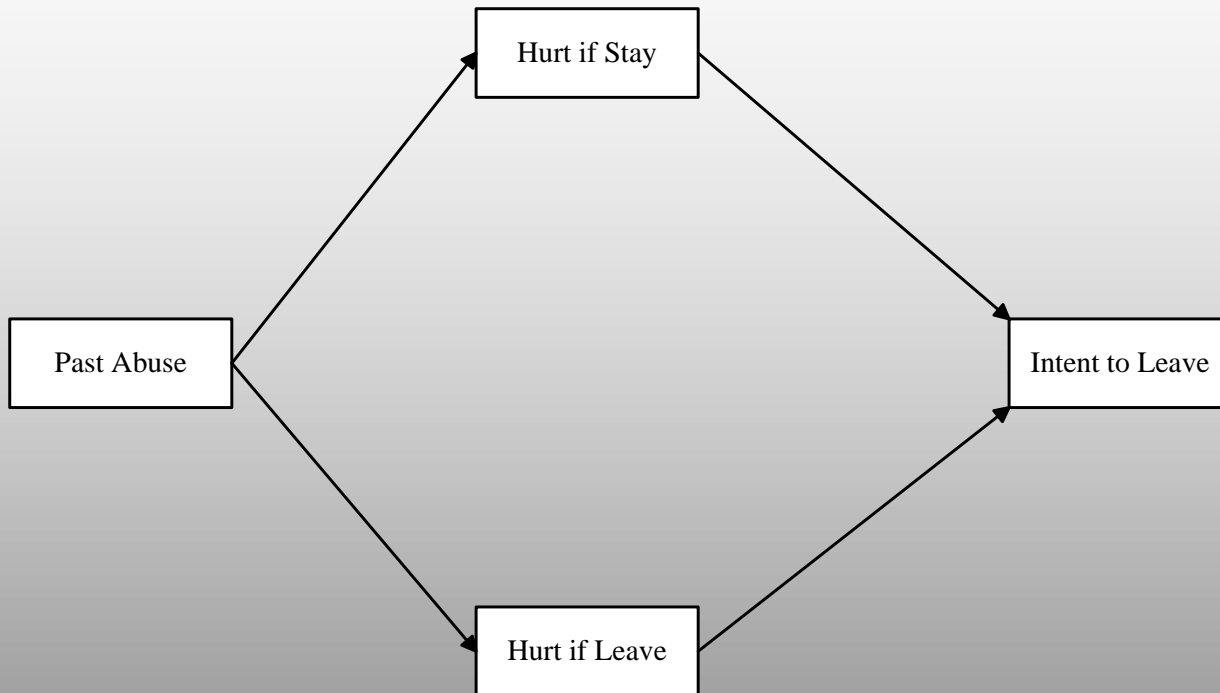
$$\text{Intent} = \alpha_1 + \beta_1 \text{ Stay} + \beta_2 \text{ Leave} + \varepsilon_3$$

# Abuse Example



$$\text{Stay} = \alpha_2 + \beta_3 \text{Abuse} + \varepsilon_1$$

# Abuse Example



$$\text{Leave} = \alpha_3 + \beta_4 \text{Abuse} + \varepsilon_2$$

# Abuse Example

The equations are:

$$\text{Intent} = \alpha_1 + \beta_1 \text{Stay} + \beta_2 \text{Leave} + \varepsilon_3$$

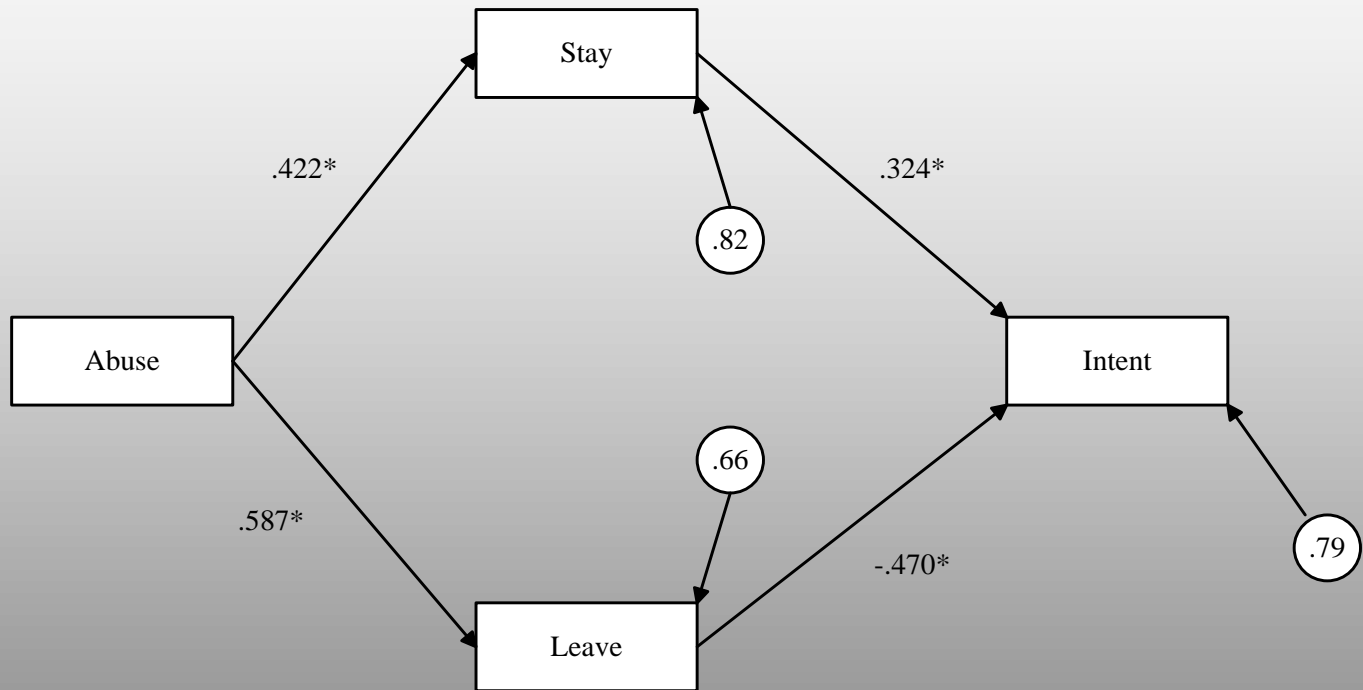
$$\text{Stay} = \alpha_2 + \beta_3 \text{Abuse} + \varepsilon_1$$

$$\text{Leave} = \alpha_3 + \beta_4 \text{Abuse} + \varepsilon_2$$

I can then estimate all the parameters using the SPSS multiple regression program, one equation at a time



# Abuse Example



# Abuse Example

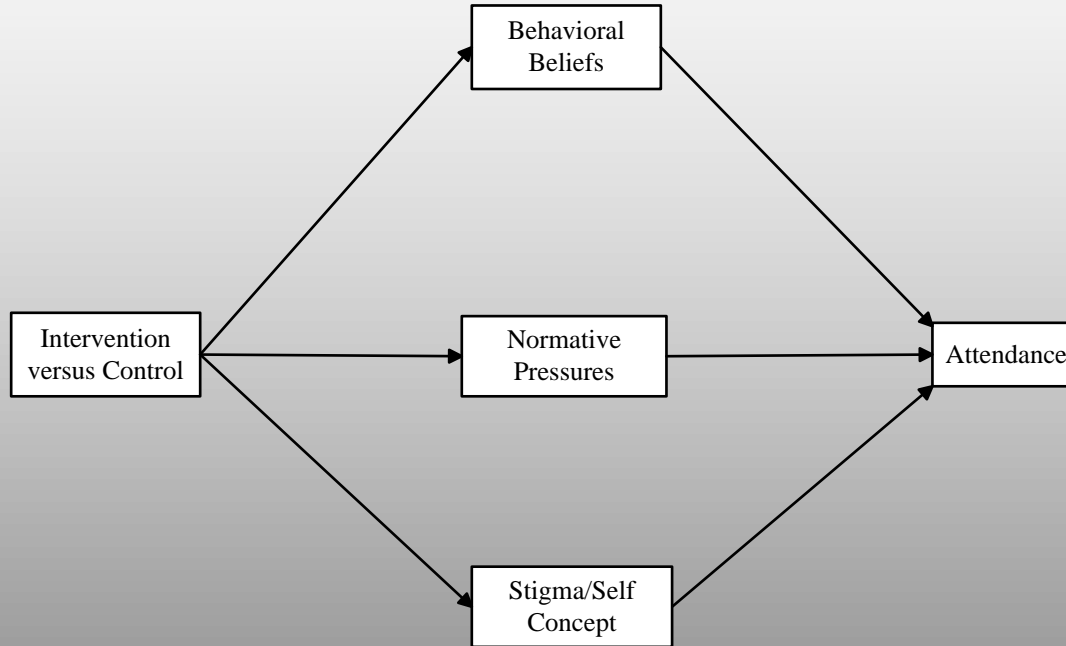
$$\text{Intent} = \alpha_1 + \beta_1 \text{Stay} + \beta_2 \text{Leave} + \varepsilon_3$$

$$\text{Stay} = \alpha_2 + \beta_3 \text{Abuse} + \varepsilon_1$$

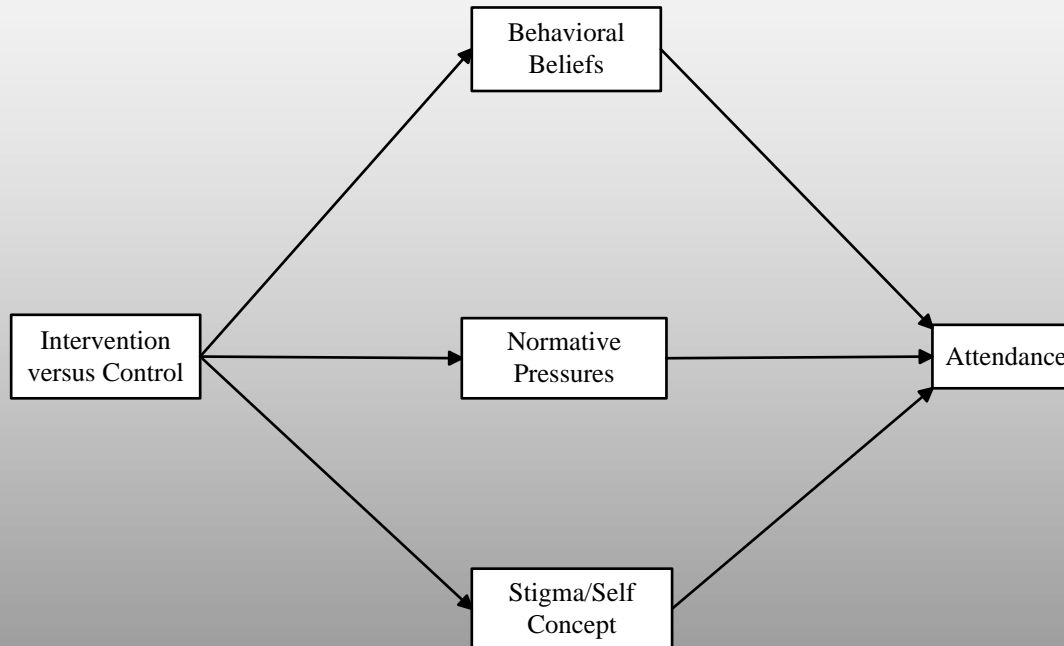
$$\text{Leave} = \alpha_3 + \beta_4 \text{Abuse} + \varepsilon_2$$

**Full information estimation estimates all coefficients simultaneously in one step. Limited information estimation chops the model up and estimates each equation separately**

# Intervention Example

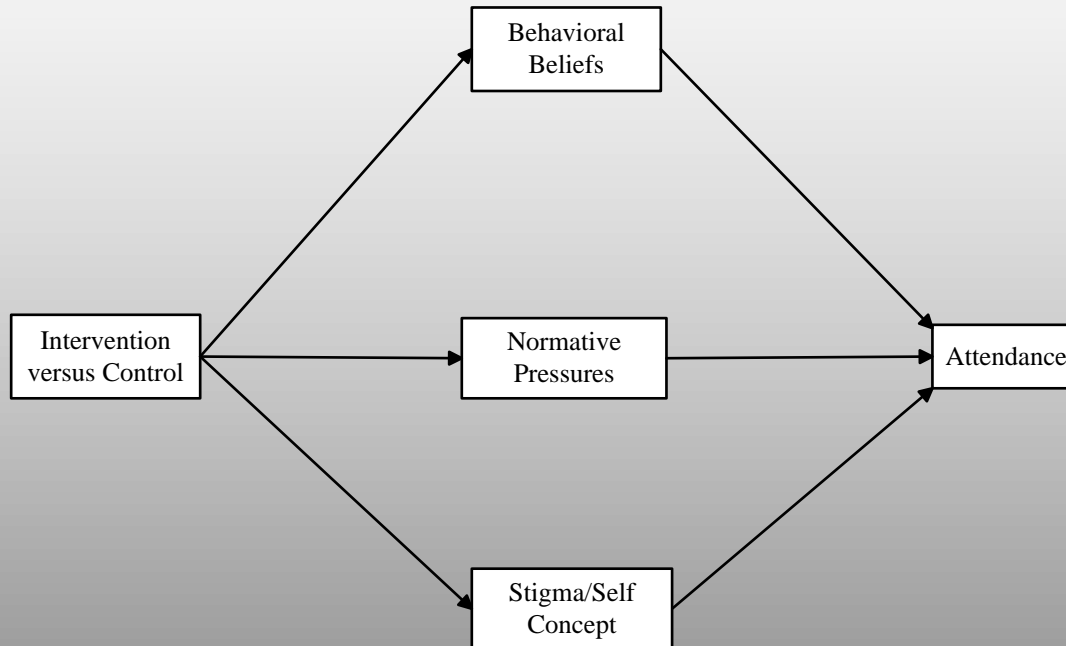


# Intervention Example



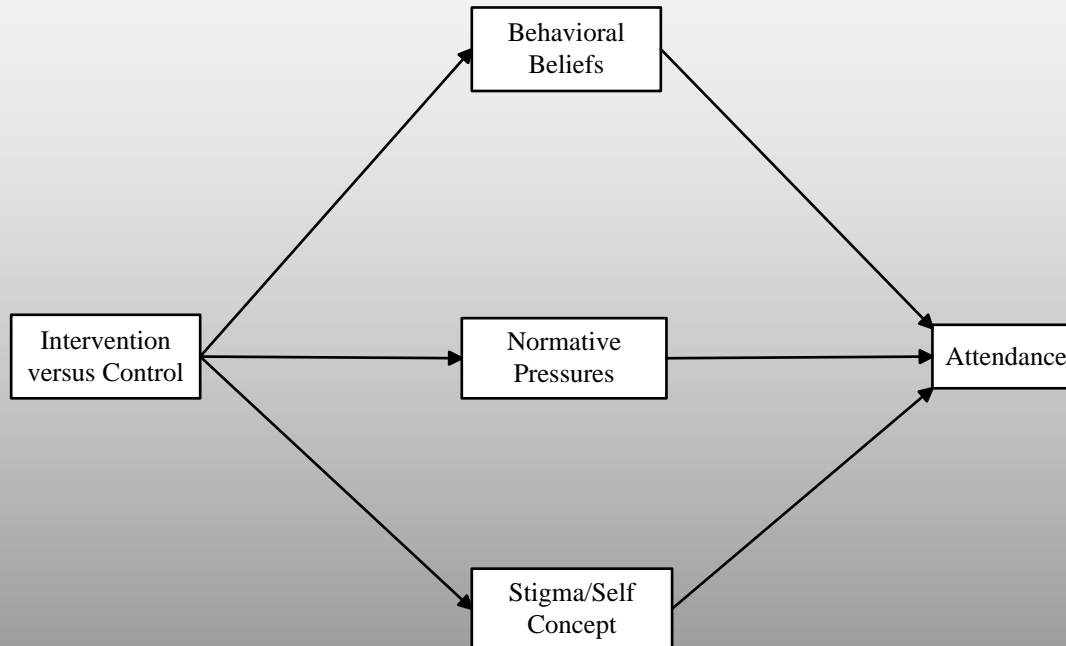
$$\text{Attendance} = \alpha_1 + \beta_1 \text{Beliefs} + \beta_2 \text{Norms} + \beta_3 \text{Stigma} + \varepsilon_4$$

# Intervention Example



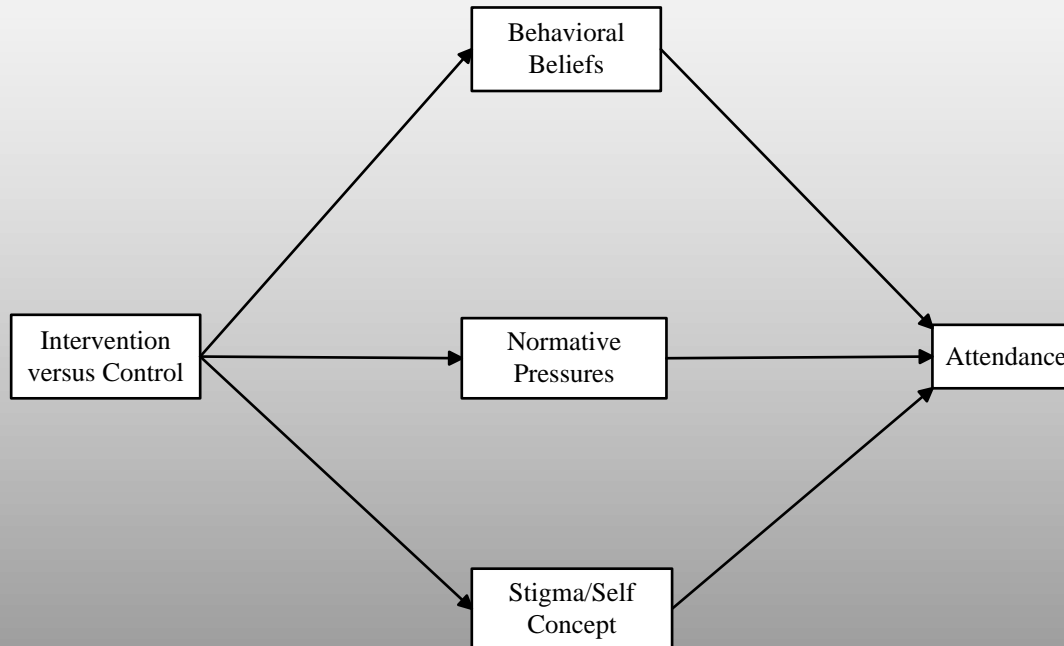
$$\text{Beliefs} = \alpha_2 + \beta_4 \text{ Intervention} + \varepsilon_1$$

# Intervention Example



$$\text{Norms} = \alpha_3 + \beta_5 \text{ Intervention} + \varepsilon_2$$

# Intervention Example



$$\text{Stigma} = \alpha_4 + \beta_6 \text{ Intervention} + \varepsilon_3$$

# Intervention Example

Putting them all together, I get:

$$\text{Attendance} = \alpha_1 + \beta_1 \text{Beliefs} + \beta_2 \text{Norms} + \beta_3 \text{Stigma} + \varepsilon_4$$

$$\text{Beliefs} = \alpha_2 + \beta_4 \text{Intervention} + \varepsilon_1$$

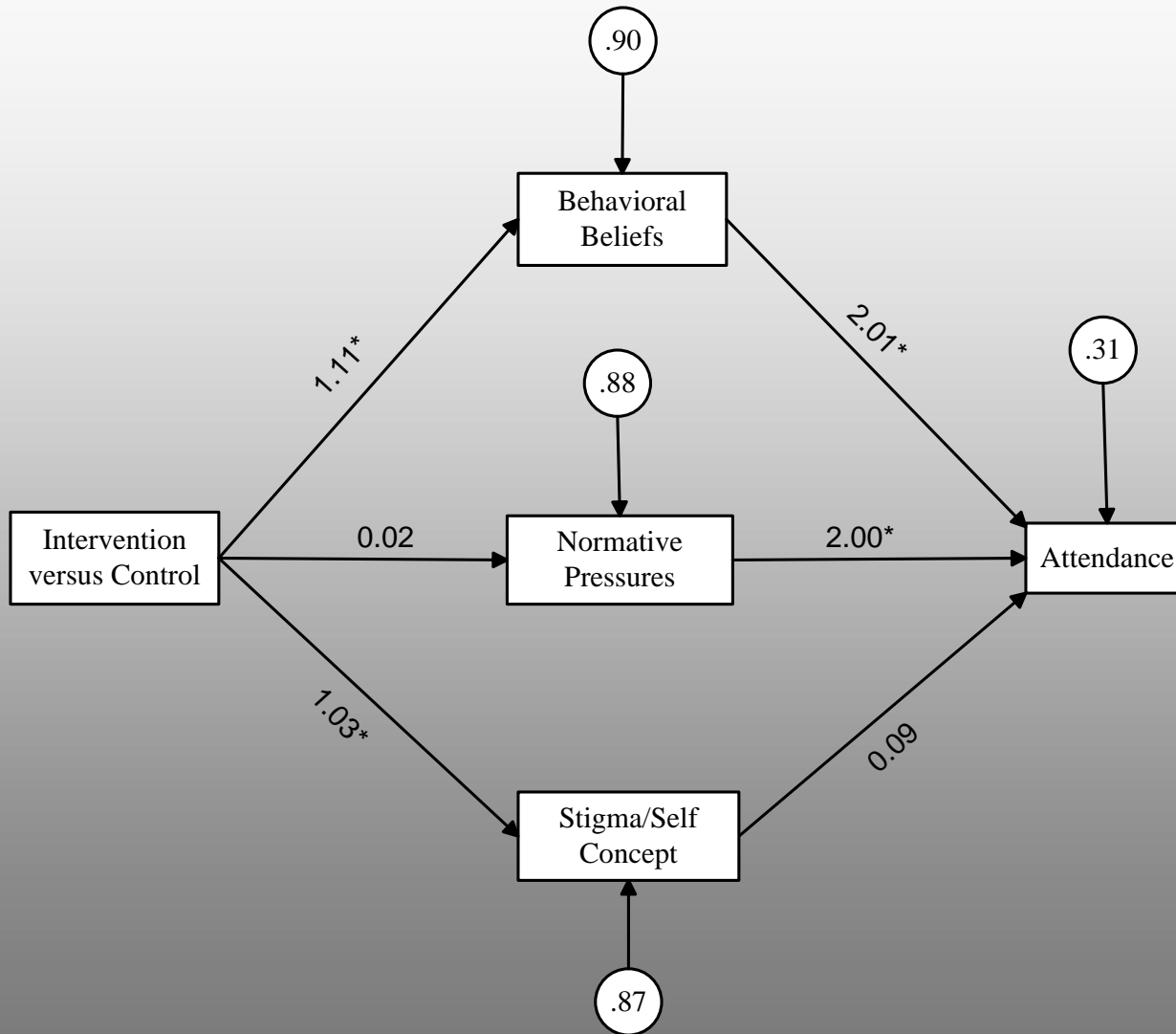
$$\text{Norms} = \alpha_3 + \beta_5 \text{Intervention} + \varepsilon_2$$

$$\text{Stigma} = \alpha_4 + \beta_6 \text{Intervention} + \varepsilon_3$$

I can then estimate all the parameters using the SPSS multiple regression program, working on one equation at a time



# Intervention Example



# Example Write-Up: Abuse Example

## Method of Analysis

The model in Figure 1 was tested using a limited information estimation strategy in conjunction with ordinary least squares (OLS) regression as applied to each of the three linear equations implied by the model. Unstandardized regression coefficients are reported in conjunction with standardized disturbance terms reflecting the proportion of unexplained variance for each endogenous variable.

## Results

Figure 1 presents the results of the three regression analyses in the form of unstandardized path coefficients and the proportion of unexplained variance for each endogenous variable. As predicted, all four of the path coefficients were statistically significant ( $p < 0.05$ ). The model is consistent with an impact of physical abuse on both the belief that staying in the relationship will result in future physical abuse and the belief that trying to leave the relationship will result in physical violence. For every one additional reported act of physical abuse in the couple's history over the course of the past 3 months, the mean belief that trying to

# Example Write-Up

leave the relationship will result in physical violence is predicted to increase by 0.37 rating scale units. History of physical abuse accounts for 34% of the variance in this belief and the associated standard error of estimate associated with the disturbance term was 0.41. Similarly, for every one additional reported act of physical abuse in the couple's history over the course of the past 3 months, the mean belief that staying in the relationship will result in future physical abuse is predicted to increase by 0.25 rating scale units. History of physical abuse accounts for 18% of the variance in this belief and the associated standard error of estimate with the disturbance term was 0.52.

The beliefs associated with being harmed if one stays or tries to leave the relationship were both statistically significantly ( $p < 0.05$ ) related to the intent to leave the relationship, accounting for 21% of the variation in intentions (the associated standard error of estimate was 0.44). For every one unit that the belief of being hurt if one stays in the relationship increased, the mean intent to leave the relationship increased by 0.32 rating scale units. For every one unit that the belief of being hurt if one tries to leave the relationship increased, the mean intent to leave the relationship decreased by 0.47 rating scale units.

# Example Write-Up

**Both of the beliefs in the model have the role of being mediators of the relationship between past abuse and the intent to leave the relationship in the next three months, as reflected by the joint significance test (MacKinnon et al., 2008).**

# Covariates

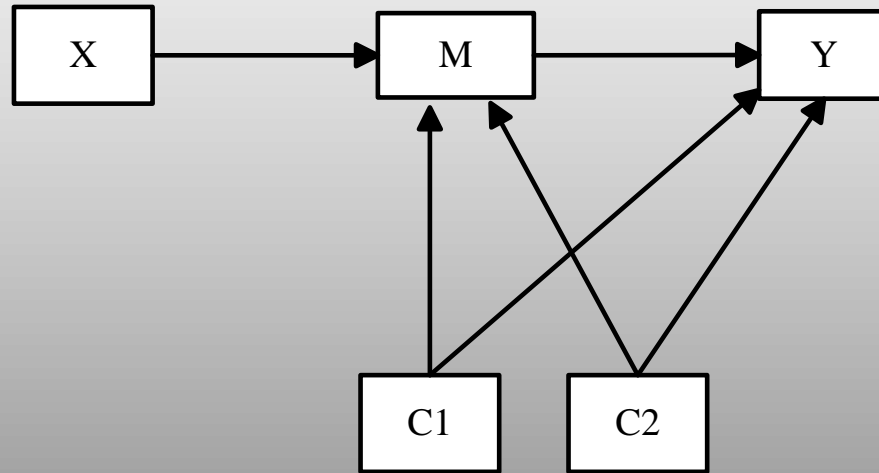
# Covariates

**We often have variables that are not part of our formal theory but that we want to control for methodological reasons.**

**We omit these variables from our formal presentations but we include them in the analysis, as per traditional covariate control in multiple regression**

**Traditionally, one controls for the covariates for each endogenous variable in the system, but this can be overridden by theoretical considerations**

# Covariates



# **Limited Information SEM**

## **Some General Advice**

**Avoid hierarchical regression**

**Be wary of standardized regression coefficients**

**(Use averaging instead of summation of items)**



# **Moderator Analysis**

**INTERACTION  
EFFECTS IN  
MULTIPLE  
REGRESSION**  
SECOND EDITION

*James Jaccard  
Robert Turrisi*

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**INTERACTION  
EFFECTS  
IN FACTORIAL  
ANALYSIS OF  
VARIANCE**

James Jaccard

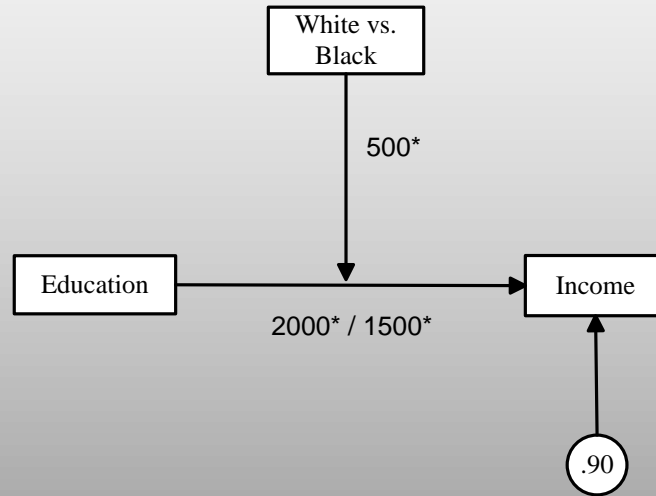
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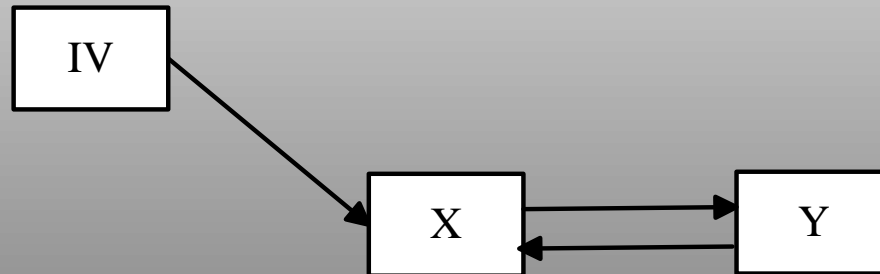
# Moderator Analysis



# Reciprocal Causation

**Uses two stage least squares regression (TSLS) or maximum likelihood methods**

**Requires instrumental variables**



# **Full Information versus Limited Information Estimation**

# **Full Information versus Limited Information**

## **Advantages of Full Information Estimation**

**Parameter estimates are more efficient**

**Can handle complex error structures more elegantly**

**Yields a more complete set of model fit indices**

**Can deal with latent variables and measurement error**



# **Full Information versus Limited Information**

## **Advantages of Limited Information**

**Less affected by model misspecification**

**More flexible in terms of mixing analytic methods (e.g., count regression, logistic regression, robust regression, ordinal regression, quantile regression, non-linear regression)**

**Less sample size demanding**

**Uses familiar methods across disciplines (e.g., dummy variables, polynomial regression)**

# Some References

**Jaccard, J., Guilamo-Ramos, V. Johansson, M. & Bouris, A. (2006). Multiple regression analyses in clinical child and adolescent psychology. *Journal of Clinical Child and Adolescent Psychology*, 35, 456-479.**

**MacKinnon, D. P., Lockwood, C. M., Hoffman, J. M., West, S. G., & Sheets, V. (2002). A comparison of methods to test the significance of the mediated effect. *Psychological Methods*, 7(1), 83–104.**

**Bollen, K.A. (2001). Two-stage least squares and latent variable models: Simultaneous estimation and robustness to misspecifications. In R. Cudeck, S. Du Toit, & D. Sörbom (Eds.), *Structural equation modeling: Present and future* (pp. 119–138). Lincolnwood, IL: Scientific Software.**

**Bollen, K.A. (1996). A limited information estimator for LISREL models with and without heteroscedasticity. In G.A. Marcoulides, & R.E. Schumacker (Eds.), *Advanced structural equation modeling* (pp. 227–241). Mahwah, NJ: Erlbaum.**